

9th meeting of

European  
Study  
Group on  
Cardiovascular  
Oscillations



# Role of Temperature and Tissue Size on Nonlinear Cardiac Dynamics

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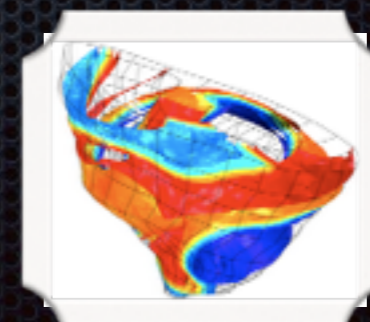
&

Flavio H. Fenton

Georgia Institute of Technology



Georgia  
Tech



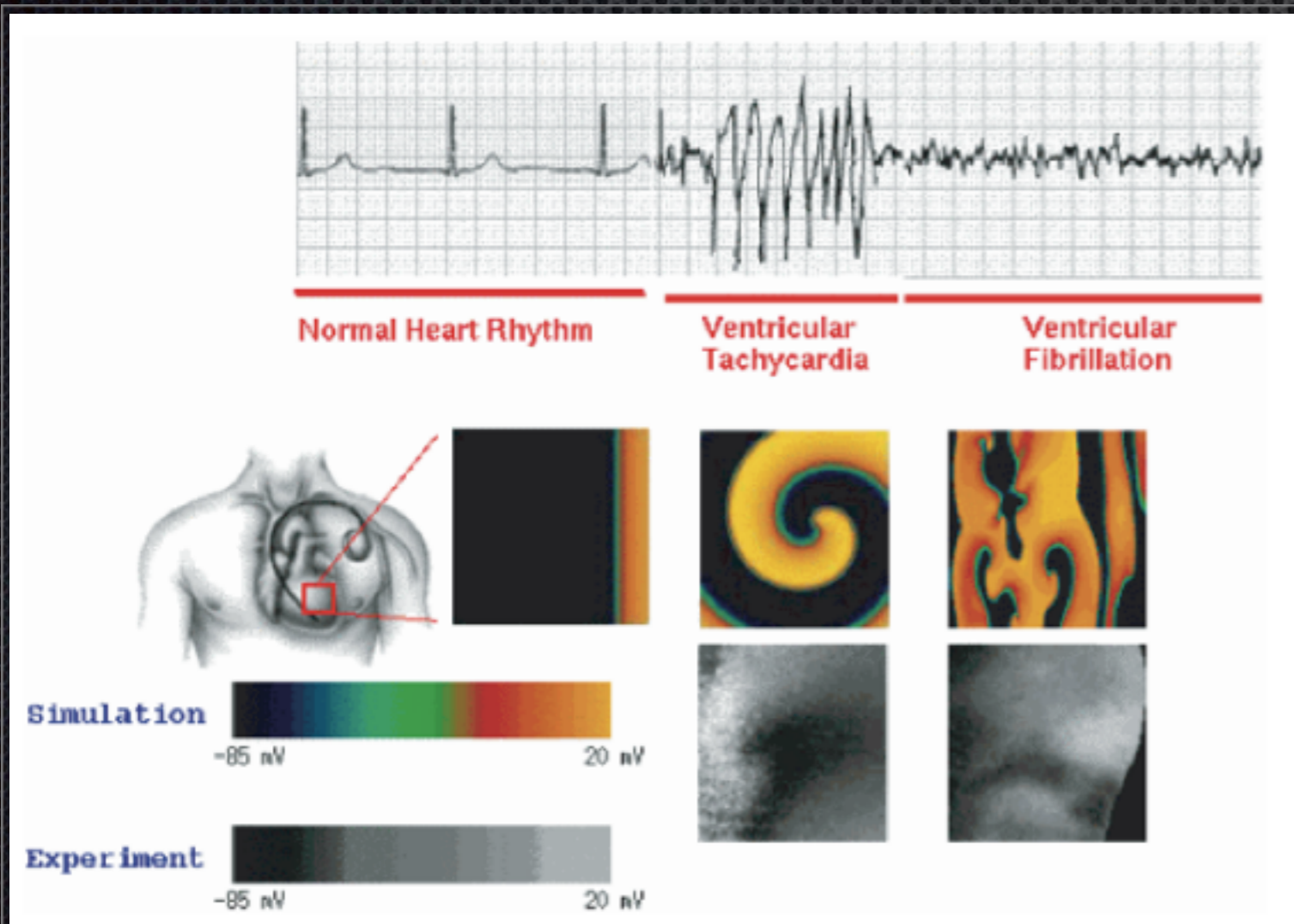
## Outline

- **Cardiac Arrhythmias and Temperature Effects**
- **Experimental Setup and Data Analysis**
- **Mathematical Modelling**
  - **Model tuning:**
    - temporal dynamics
    - spatio-temporal dynamics
  - **Alternans:** bifurcation analysis
  - **Arrhythmias:**
    - domain size and temperature effects
- **Conclusions**

# Cardiac Arrhythmias

## Cardiac Rhythm Transition

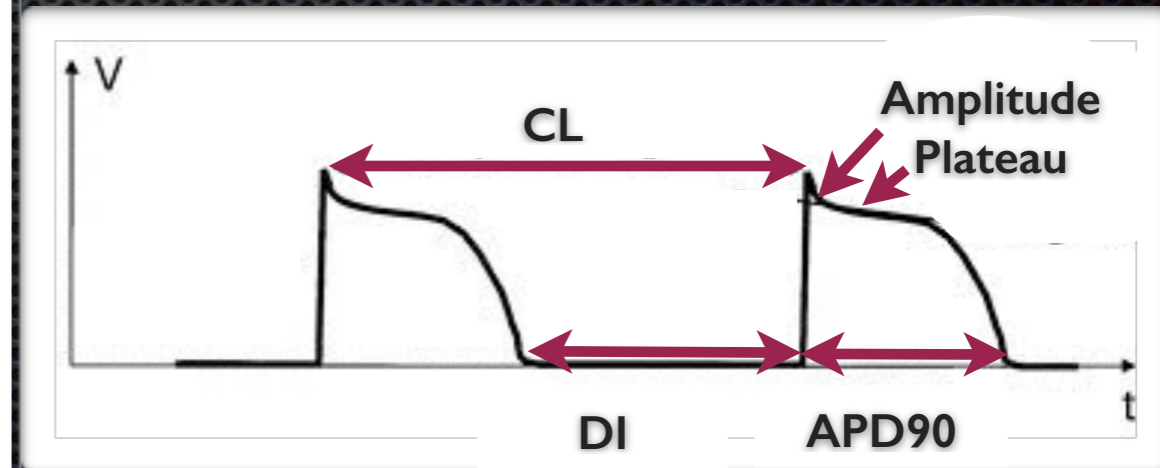
The 'standard' induction of Ventricular Fibrillation measured via the ECG goes from Normal Rhythm - to - Ventricular Tachycardia - to - Ventricular Fibrillation



## Cardiac Alternans

### Restitution Curves

- APD vs. CL
- APD vs. DI
- CV vs. CL
- CV vs. DI

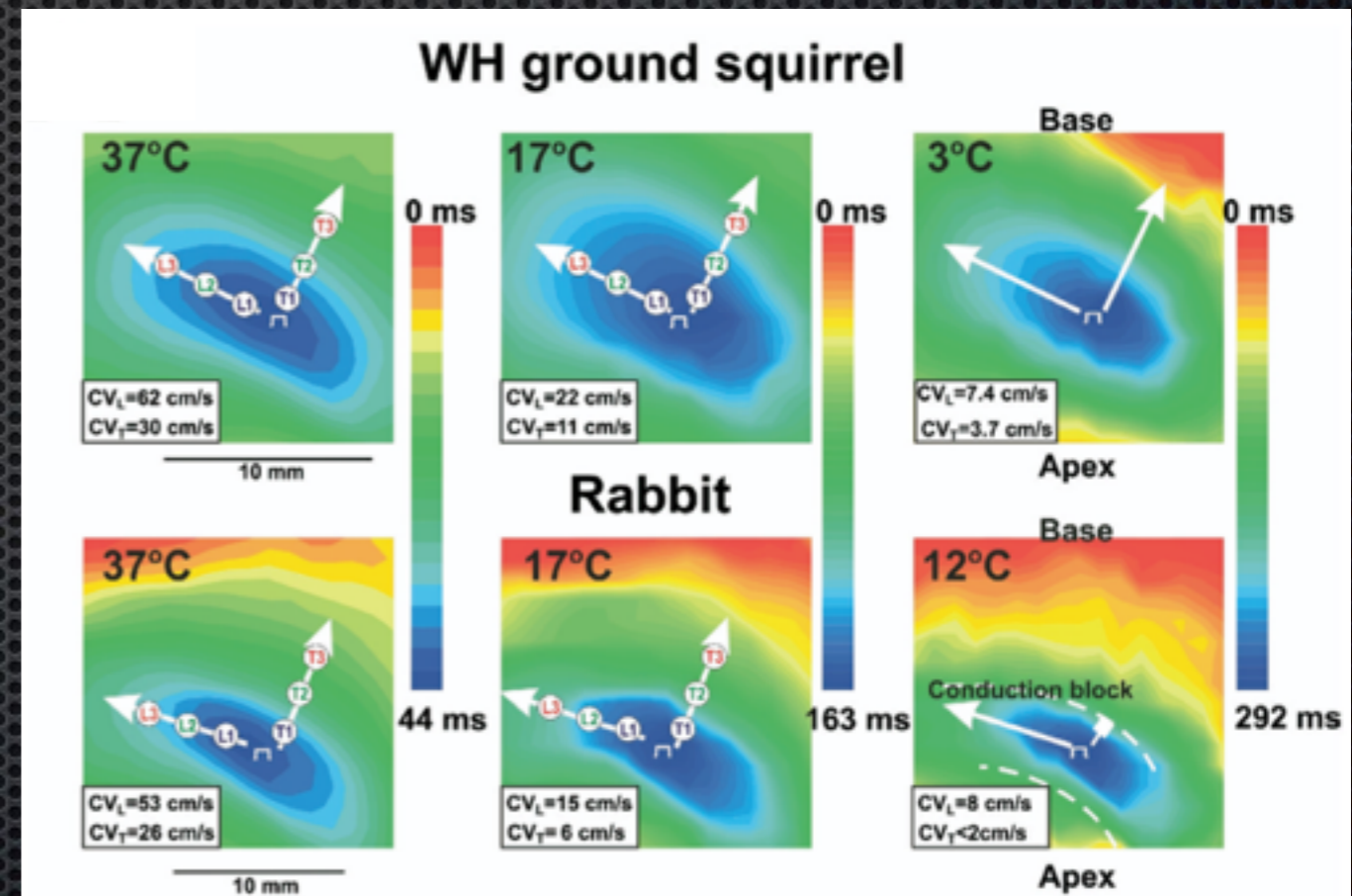
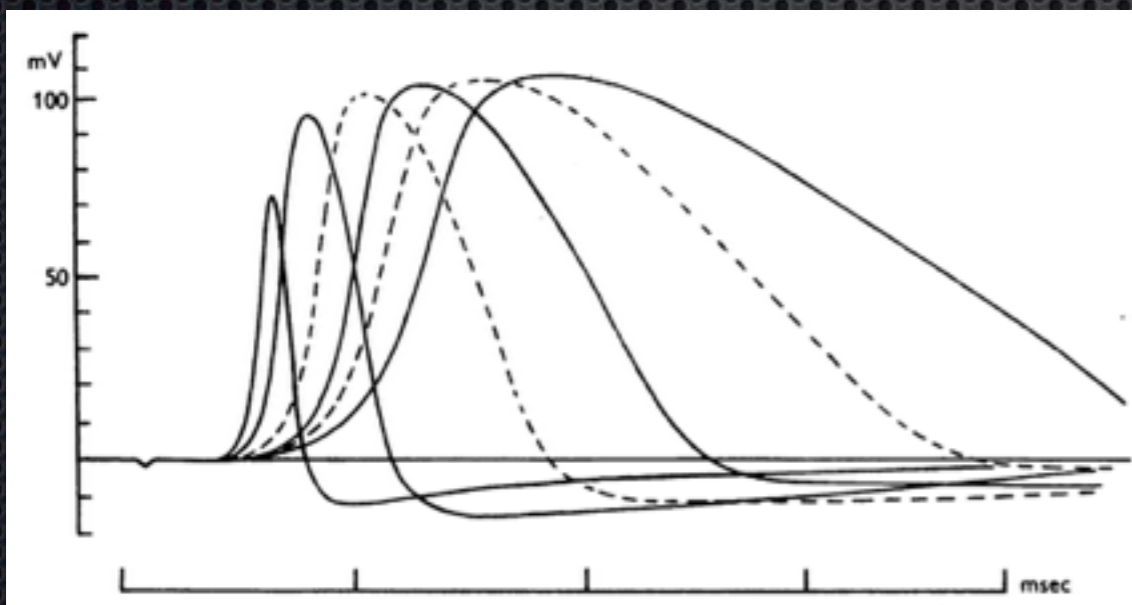
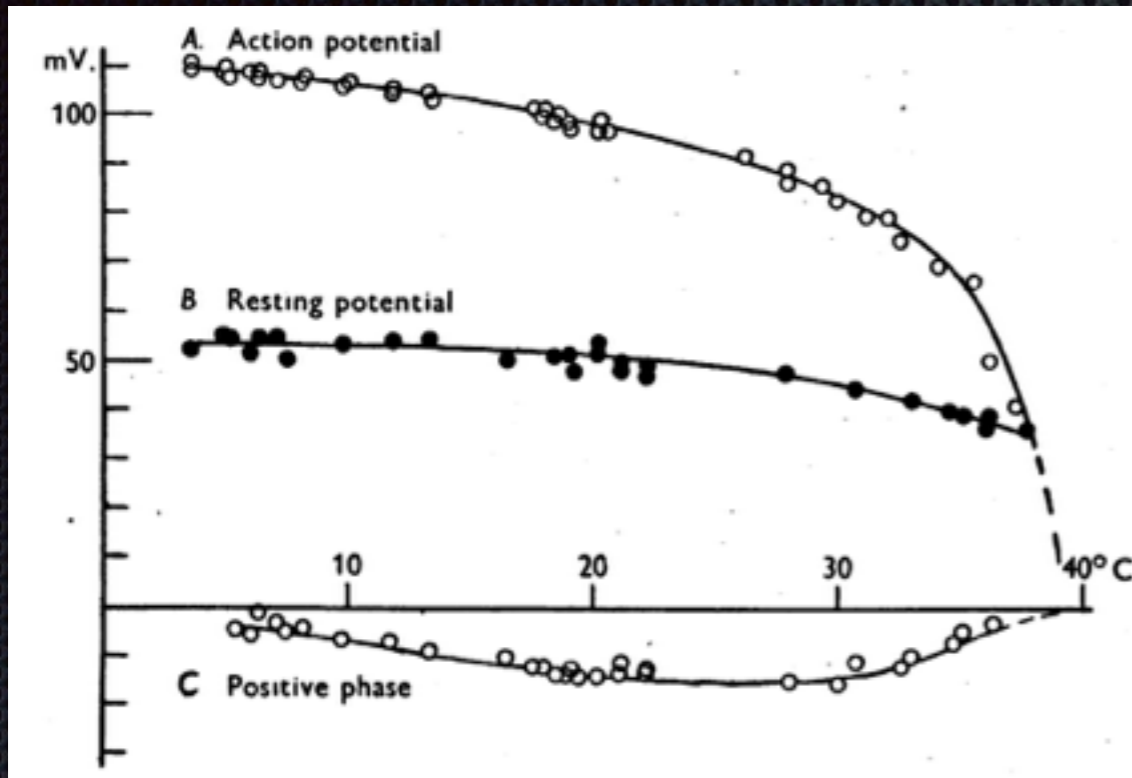


Fenton Scholarpedia 2008

# Temperature Effects on Excitable Systems

## Effects of Temperature

- ▶ APD duration
- ▶ Frequency
- ▶ Excitability threshold
- ▶ Spatio-Temporal behaviours...

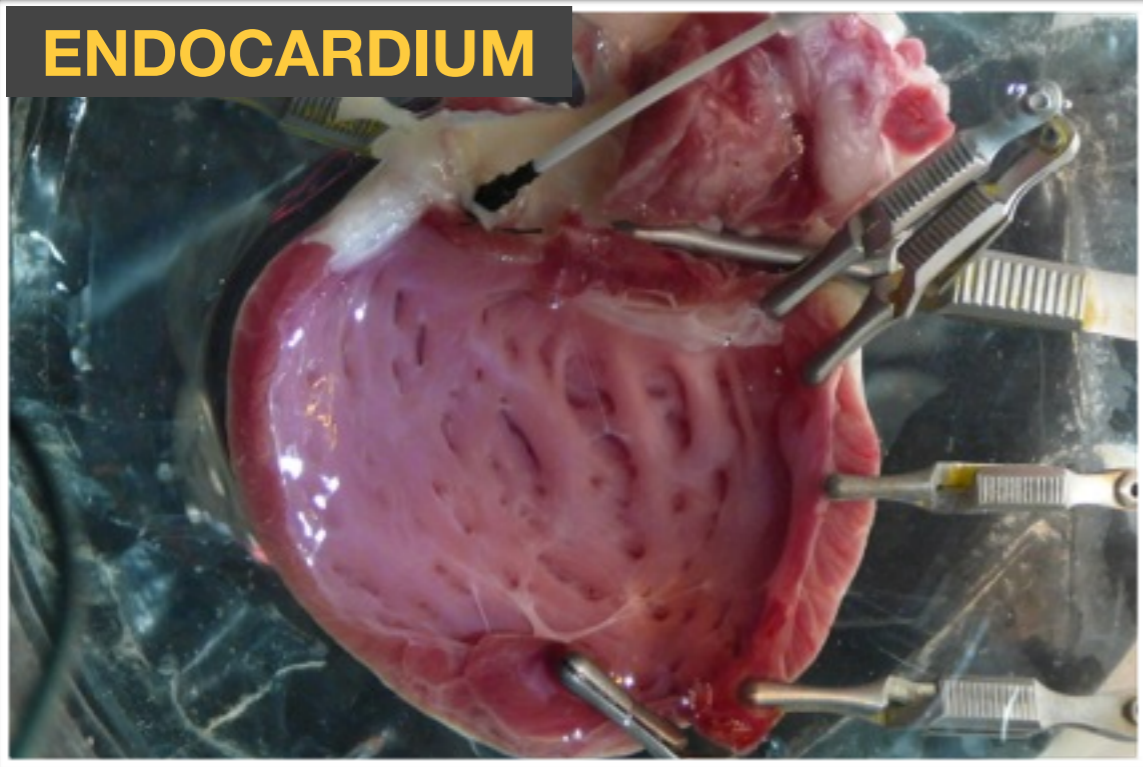


Hodgkin, A. L., & Katz, B. (1949). *The Journal of physiology*, 109(1-2), 240.

Fedorov, V. V., Glukhov, A. V., Sudharshan, S., Egorov, Y., Rosenshtraukh, L. V., & Efimov, I. R. (2008). *Heart Rhythm*, 5(11), 1587-1596.

# Experimental Setup

**ENDOCARDIUM**



**EPICARDIUM**



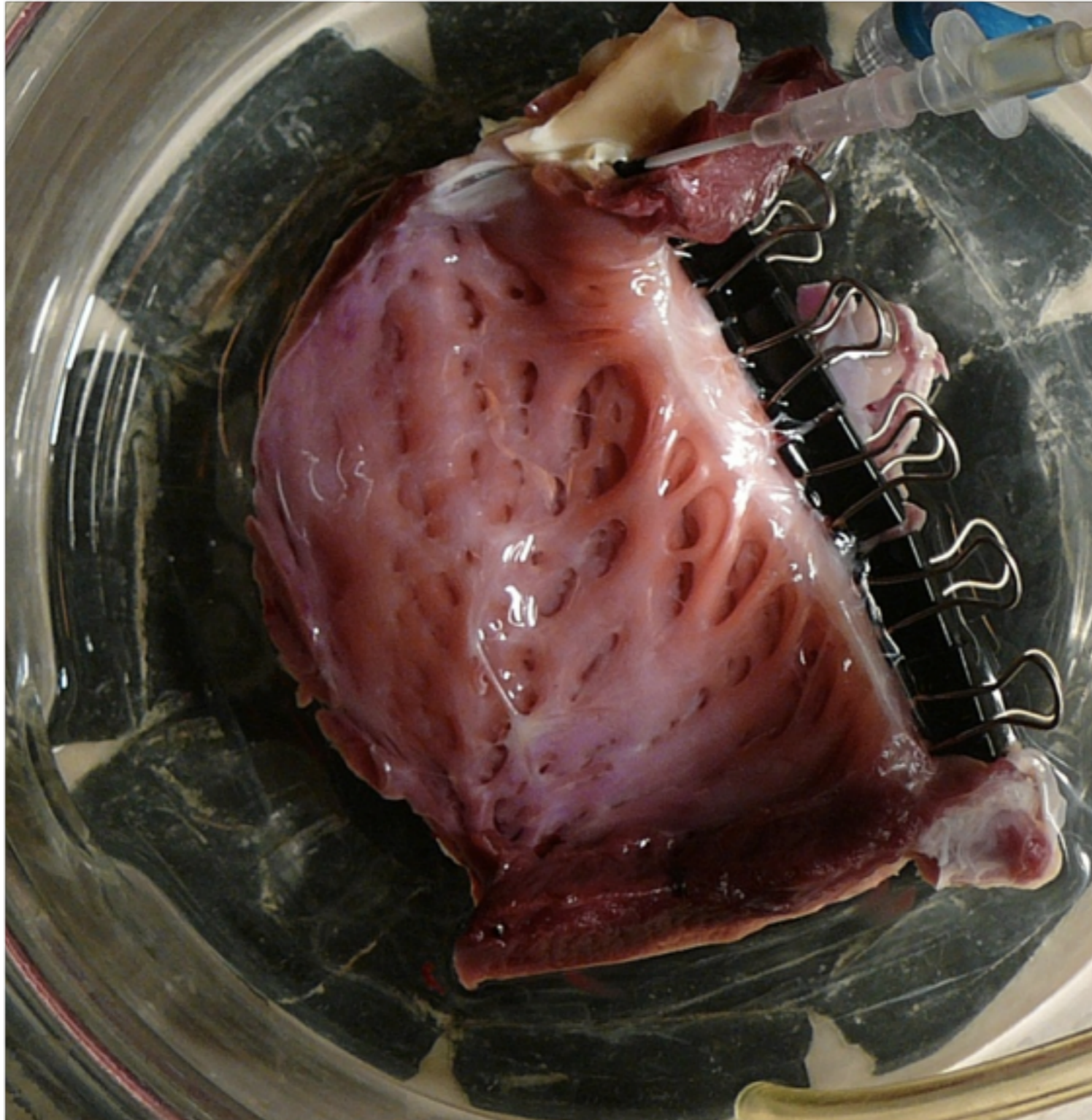
## PROTOCOL

- Canine heart excised, right ventricle isolation and cannulation
- Tyrode solution with Voltage-Sensitive Dye (Di-4-ANEPPS) equilibration (37°C)
- Blebbistatin
- Selected light emission (530 nm)
- Endocardial stimulation
- Endo-Epi synchronous recording (2 ms/frame, 128x128 pixels, 600 μm/pixel)



# Experimental Setup

- **IN VITRO OPTICAL MAPPING RECORDINGS**

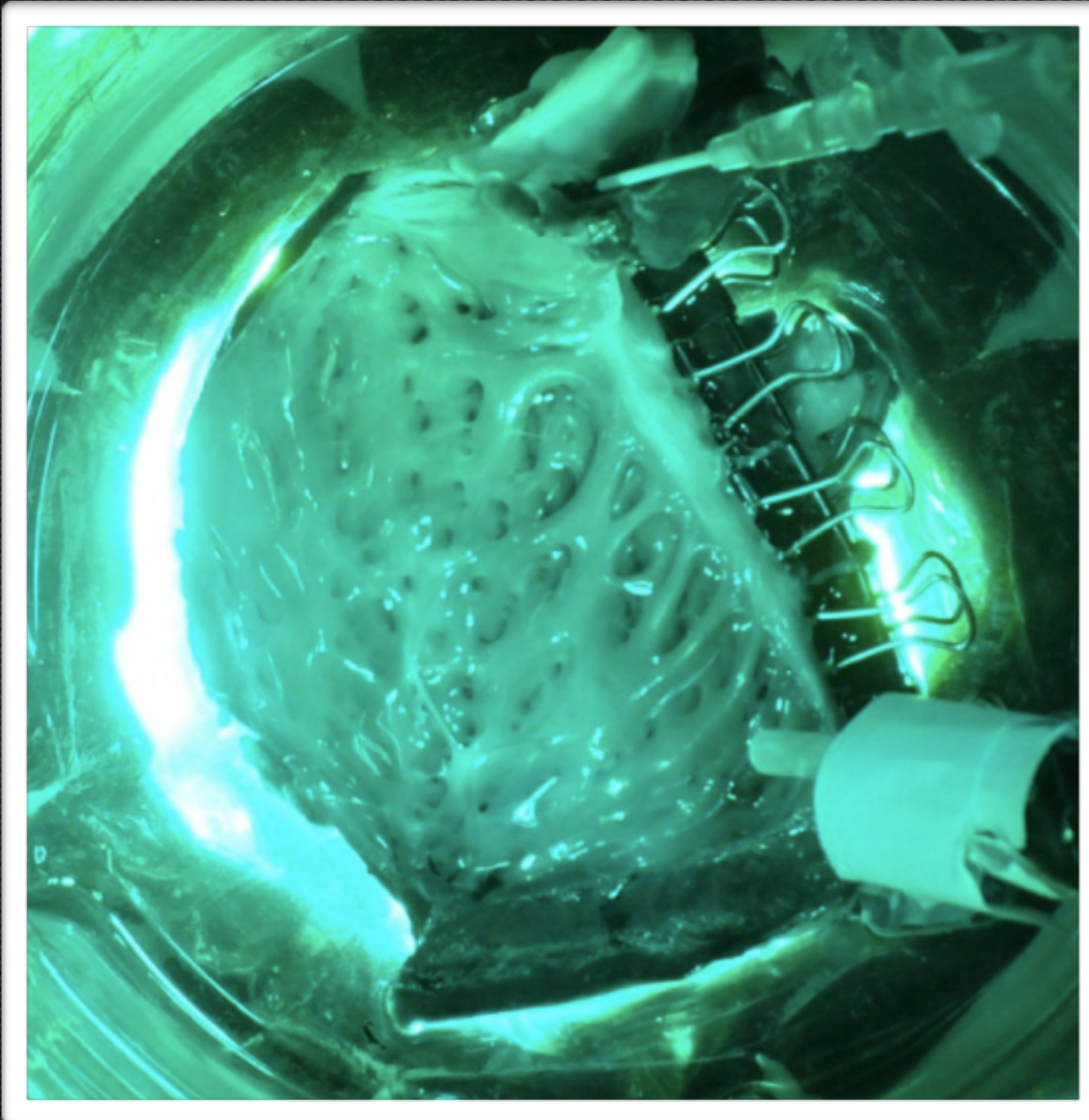


**Original  
Tissue**



# Experimental Setup

- **IN VITRO OPTICAL MAPPING RECORDINGS**



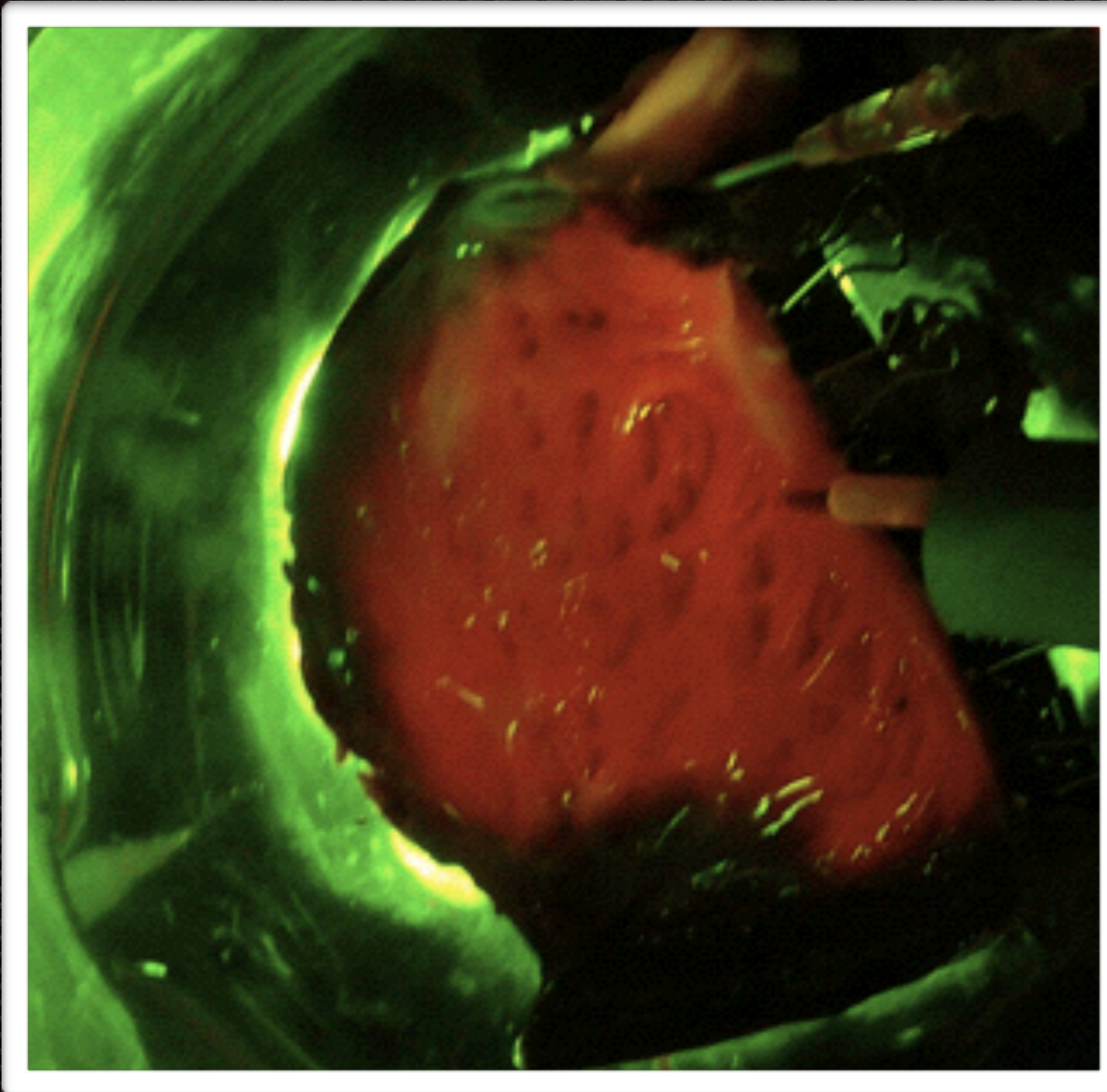
Original  
Tissue

Illuminated  
Tissue



# Experimental Setup

- **IN VITRO OPTICAL MAPPING RECORDINGS**



**Original  
Tissue**

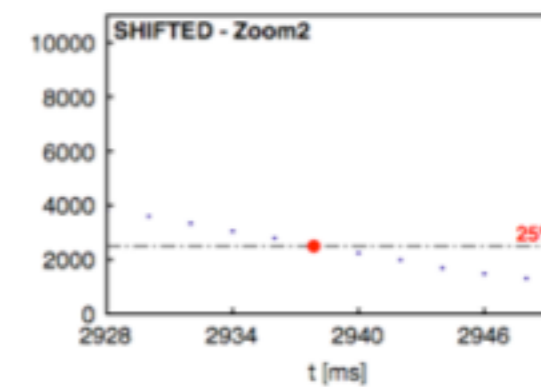
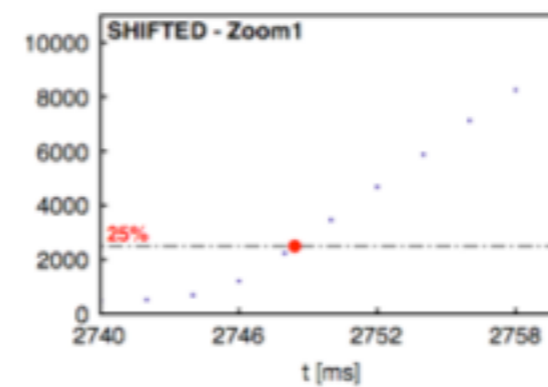
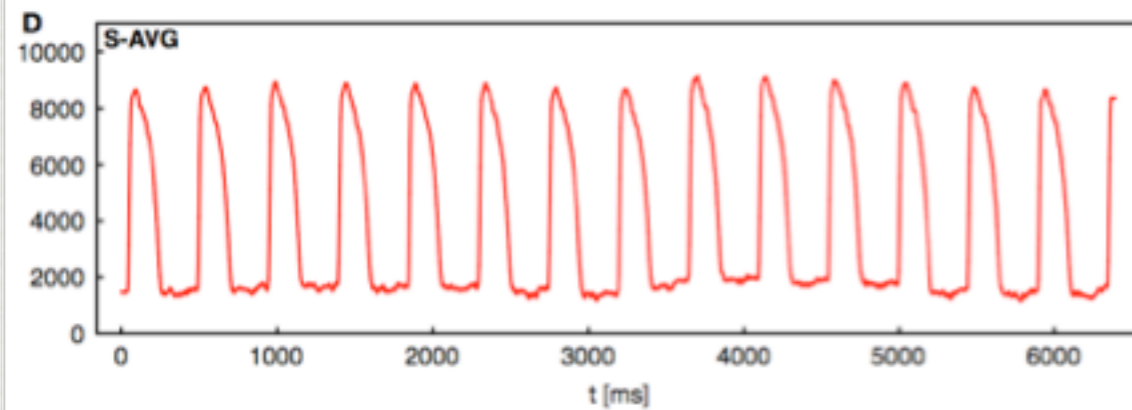
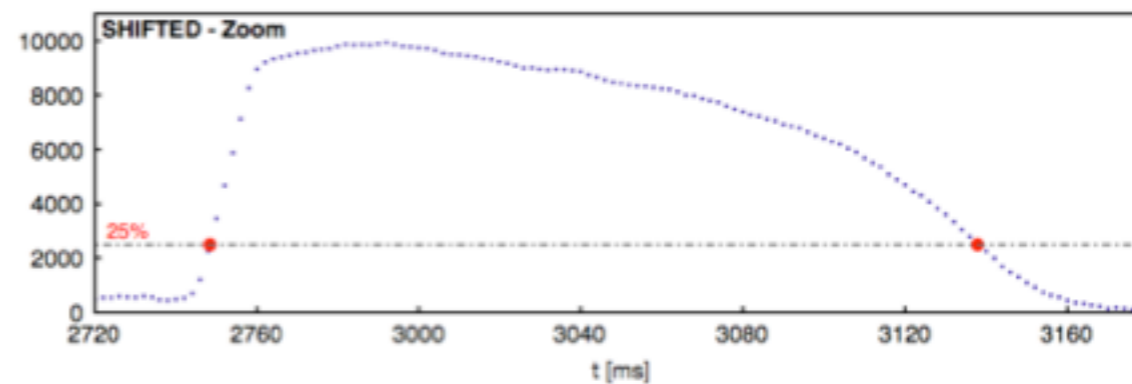
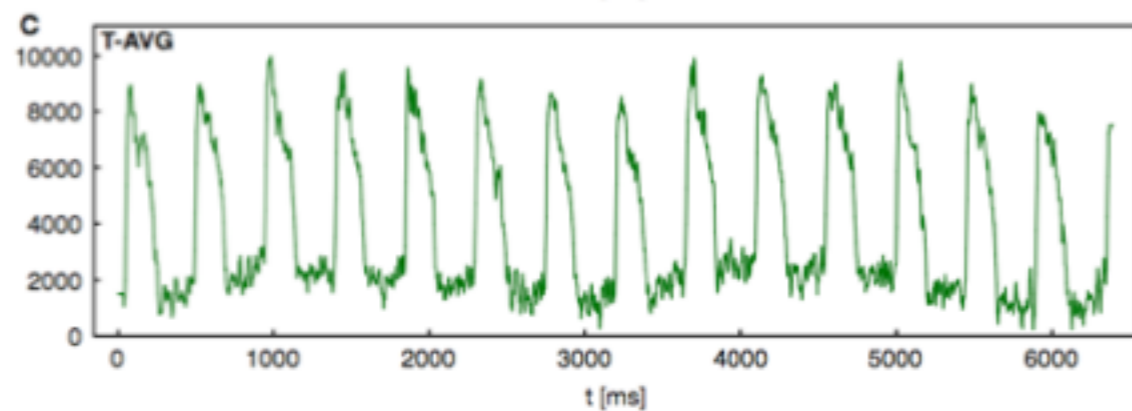
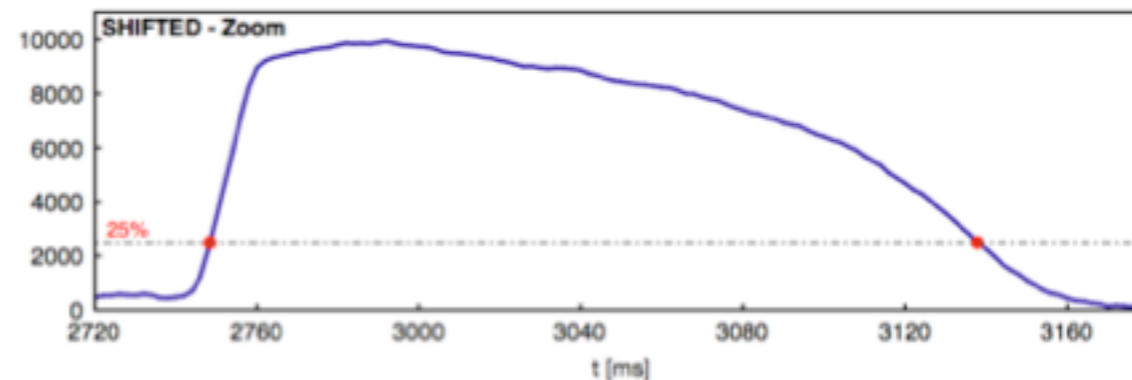
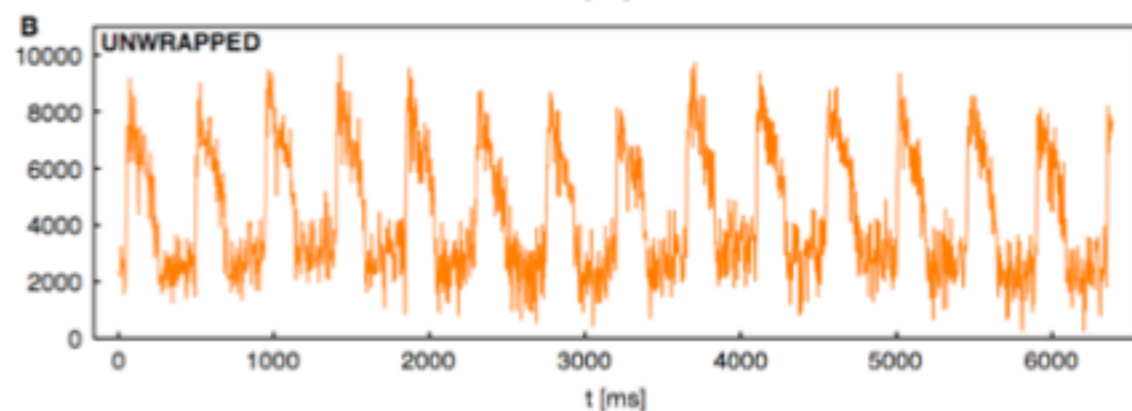
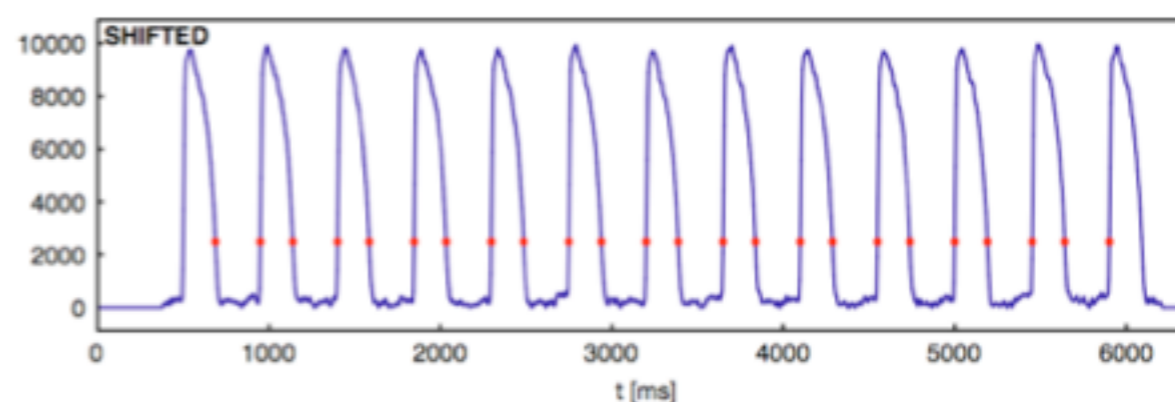
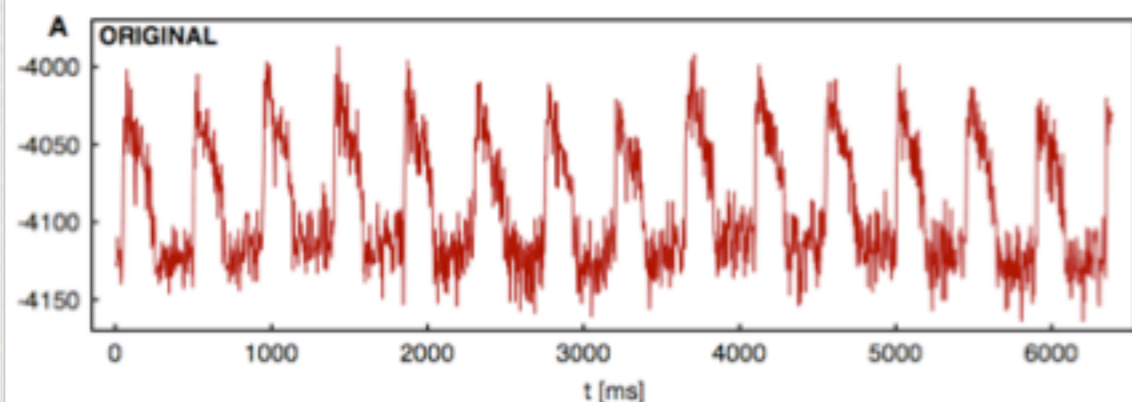
**Illuminated  
Tissue**

**Fluorescent  
Signal**





# Experimental Data Analysis

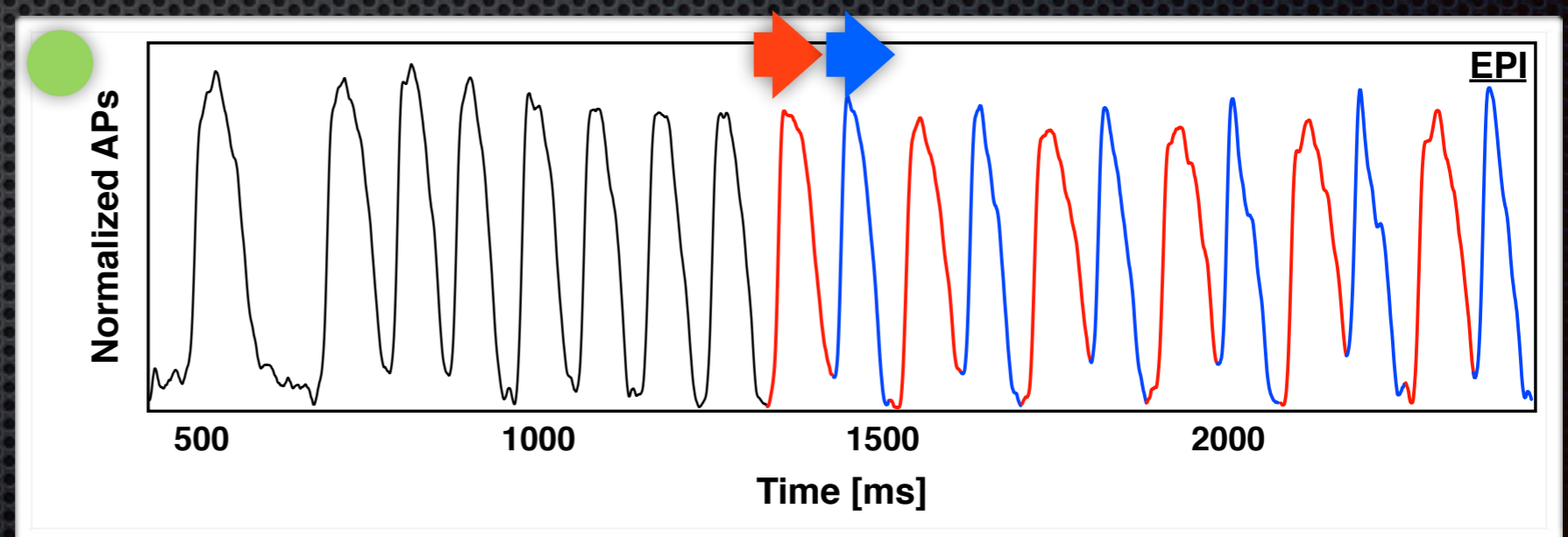
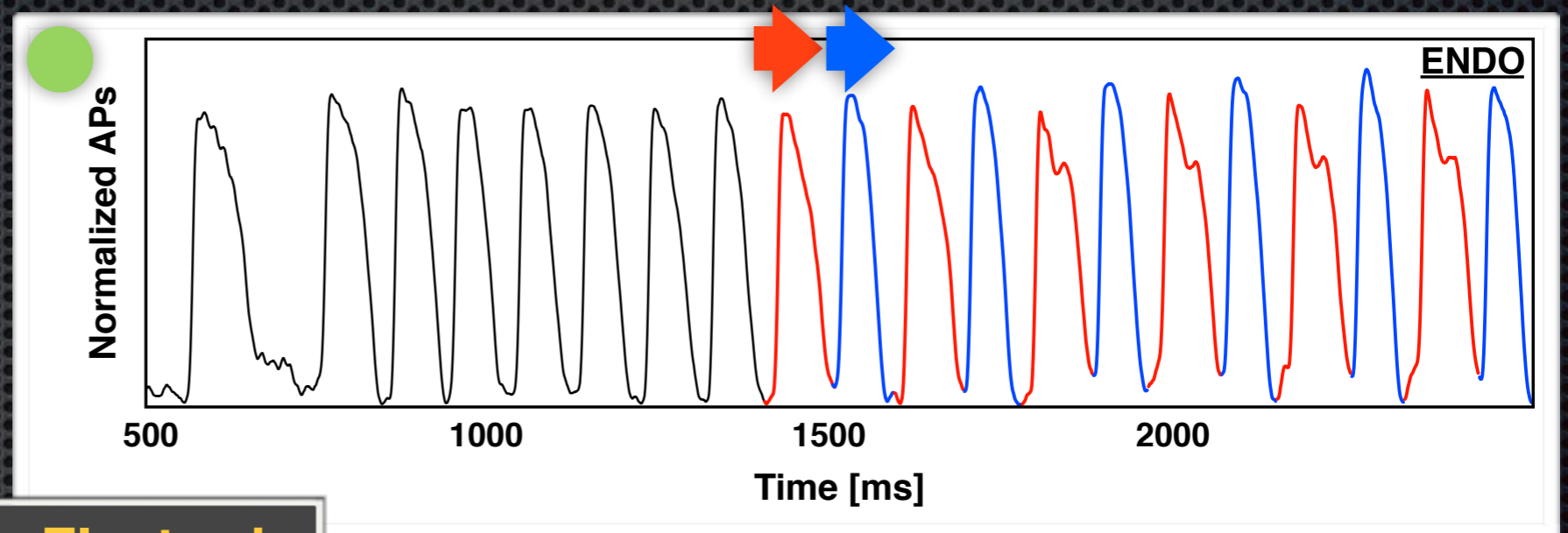


# Experimental Data Analysis

- **Development:** constant pacing Cycle Length (CL=160ms)

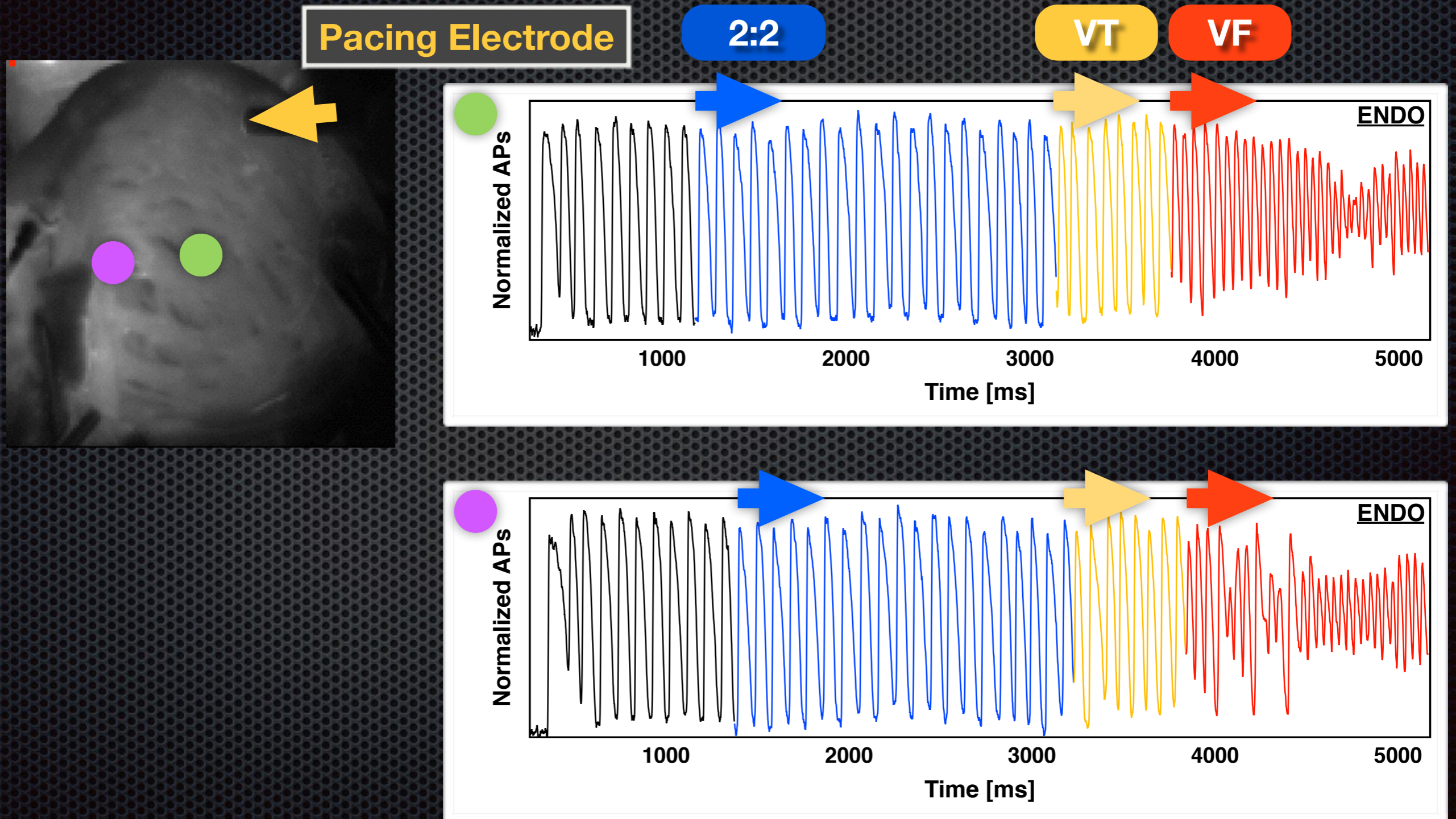


**Pacing Electrode**



# Experimental Data Analysis

- Development into **VF** with a transition in **VT** (CL=160ms)



# Mathematical Model

## Phenomenological Minimal Model for Human Action Potential (Bueno-Orovio et al. 2008)

$$\begin{aligned} \partial_t u &= D\nabla^2 u - (J_{fi} + J_{so} + J_{si}), & (1) \\ \partial_t v &= \phi_v(T) \left[ [1 - H(u - \theta_v)] \frac{(v_\infty - v)}{\tau_v^-} - \frac{H(u - \theta_v)v}{\tau_v^+} \right], & (2) \\ \partial_t w &= \phi_w(T) \left[ [1 - H(u - \theta_w)] \frac{(w_\infty - w)}{\tau_w^-} - \frac{H(u - \theta_w)w}{\tau_w^+} \right], & (3) \\ \partial_t s &= \phi_s(T) \left[ \frac{[1 + \tanh[k_s(u - u_s)]]/2 - s}{\tau_s} \right], & (4) \\ J_{fi} &= \eta_{fi}(T) \left[ -H(u - \theta_v)(u - \theta_v)(u_u - u) \frac{v}{\tau_{fi}} \right], & (5) \\ J_{so} &= \eta_{so}(T) \left[ [1 - H(u - \theta_w)] \frac{(u - u_o)}{\tau_o} + \frac{H(u - \theta_w)}{\tau_{so}} \right], & (6) \\ J_{si} &= \eta_{si}(T) \left[ -H(u - \theta_w) \frac{ws}{\tau_{si}} \right], & (7) \end{aligned}$$

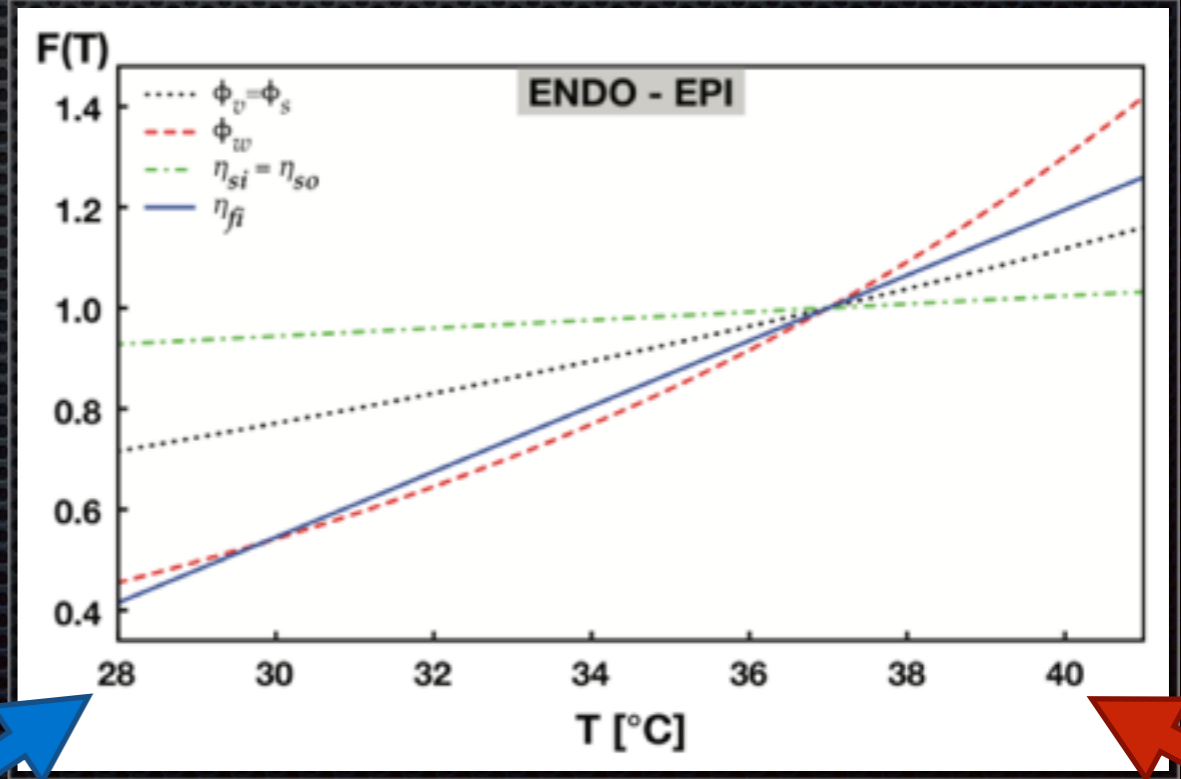
$$\begin{aligned} \tau_v^-(u) &= [1 - H(u - \theta_v^-)]\tau_{v1}^- + H(u - \theta_v^-)\tau_{v2}^-, & (8) \\ \tau_w^+(u) &= \tau_{w1}^+ + (\tau_{w2}^+ - \tau_{w1}^+) \frac{\tanh[k_w^+(u - u_w^+)] + 1}{2}, & (9) \\ \tau_w^-(u) &= \tau_{w1}^- + (\tau_{w2}^- - \tau_{w1}^-) \frac{\tanh[k_w^-(u - u_w^-)] + 1}{2}, & (10) \\ \tau_{so}(u) &= \tau_{so1} + (\tau_{so2} - \tau_{so1}) \frac{\tanh[k_{so}(u - u_{so})] + 1}{2}, & (11) \\ \tau_s(u) &= [1 - H(u - \theta_w)]\tau_{s1} + H(u - \theta_w)\tau_{s2}, & (12) \\ \tau_o(u) &= [1 - H(u - \theta_o)]\tau_{o1} + H(u - \theta_o)\tau_{o2}. & (13) \end{aligned}$$

$$\begin{aligned} v_\infty &= \begin{cases} 1, & u < \theta_v^- \\ 0, & u \geq \theta_v^- \end{cases} & (14) \\ w_\infty &= [1 - H(u - \theta_o)] \left(1 - \frac{u}{\tau_{w\infty}}\right) + H(u - \theta_o)w_\infty^*, & (15) \end{aligned}$$

PHYSICAL REVIEW E 87, 042717 (2013)  
**Role of temperature on nonlinear cardiac dynamics**  
 Flavio H. Fenton,<sup>1</sup> Alessio Gizzi,<sup>2,3</sup> Christian Cherubini,<sup>2,4</sup> Nicola Pomella,<sup>2,3</sup> and Simonetta Filippi<sup>2,4</sup>

$$\begin{aligned} \phi(T) &= Q_{10}^{(T-T_a)/10}, \\ \eta(T) &= A[1 + B(T - T_a)]. \end{aligned}$$

**Arrhenius**  
**Moore**



**Changes on the Time Constants**

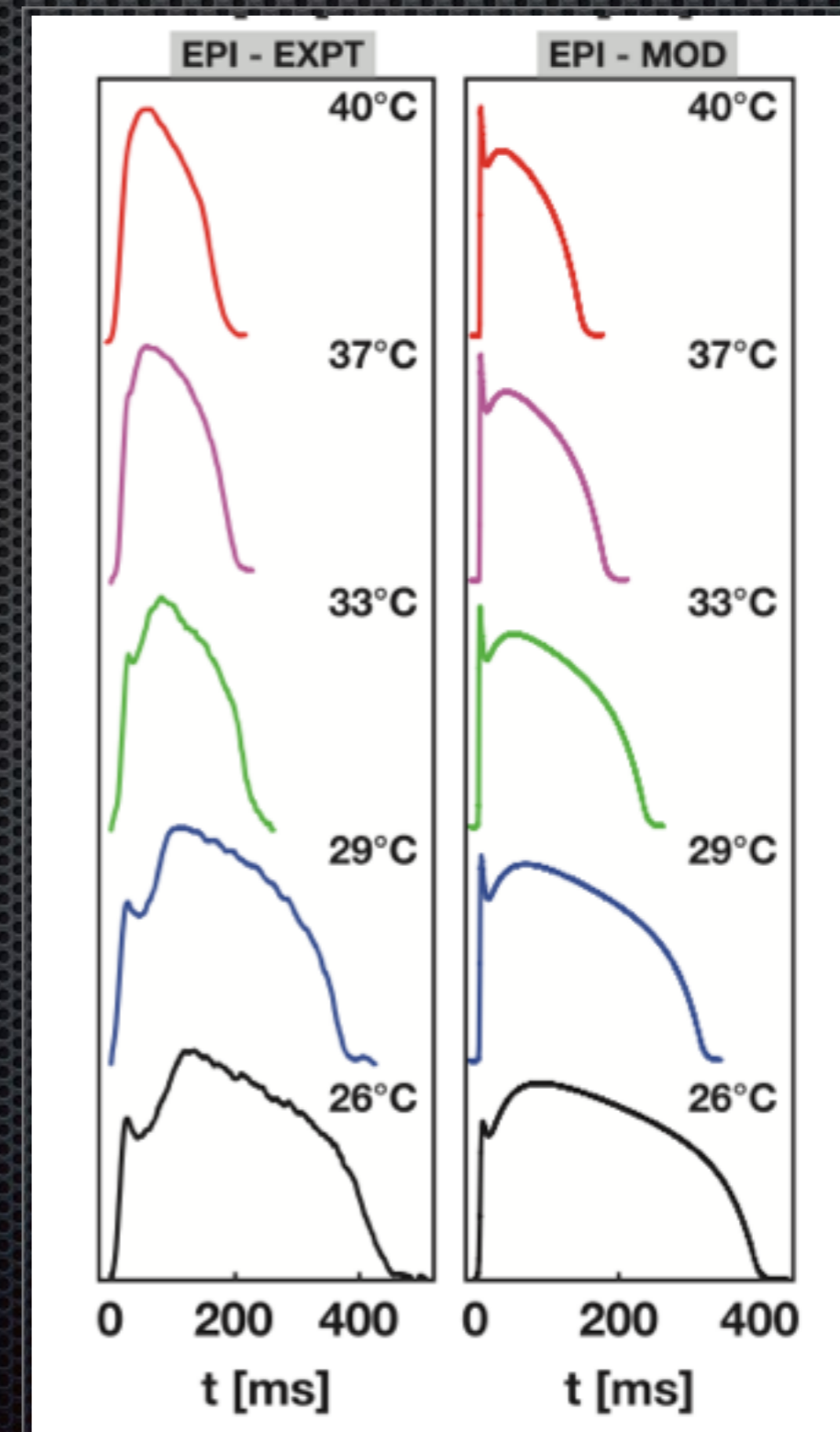
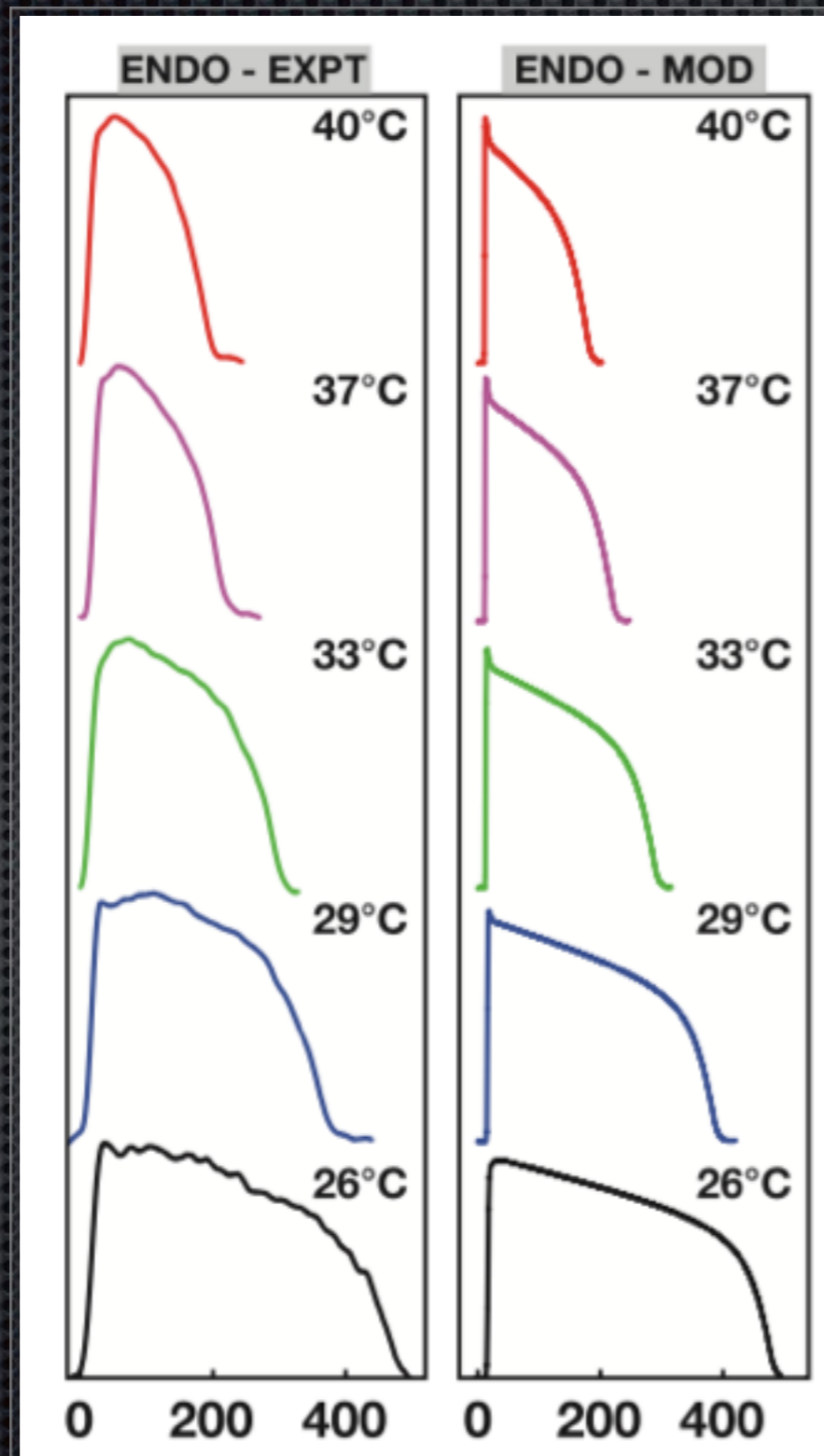
**Motivated on Experimental Setup**



# Model Tuning

Action Potential Shape Fitting

Qualitative Matching

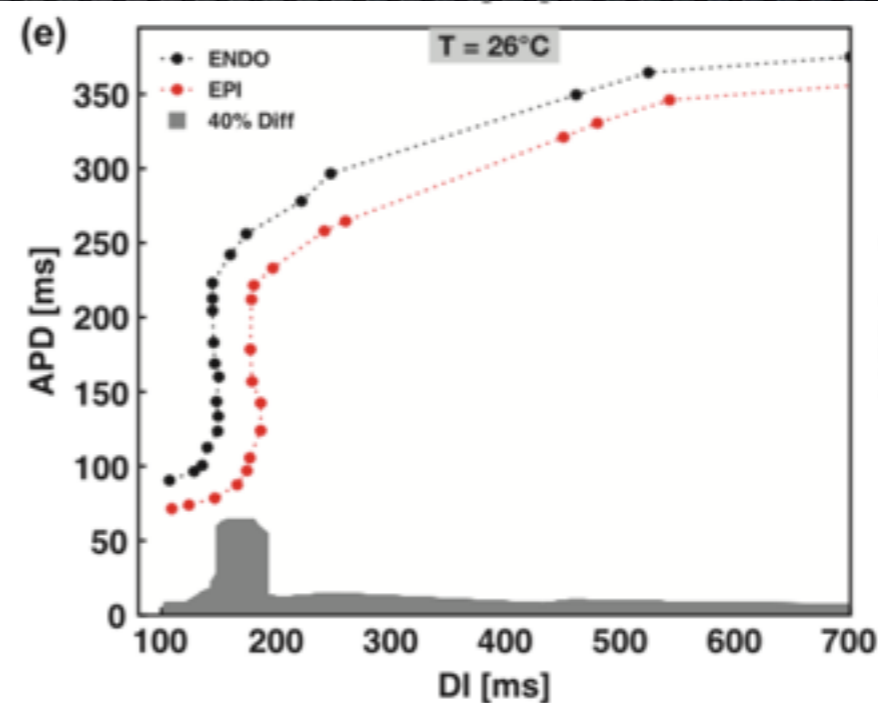
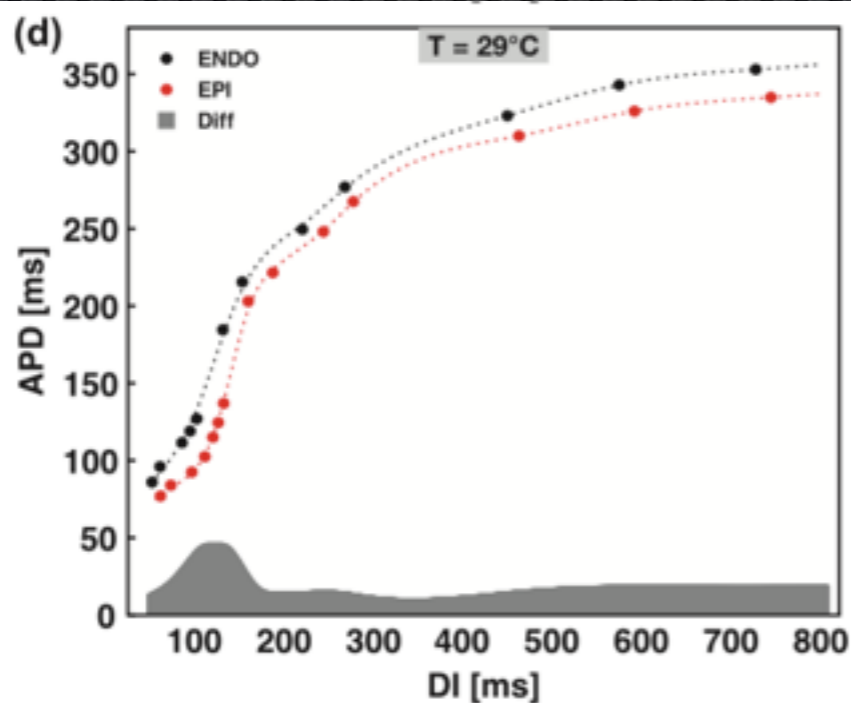
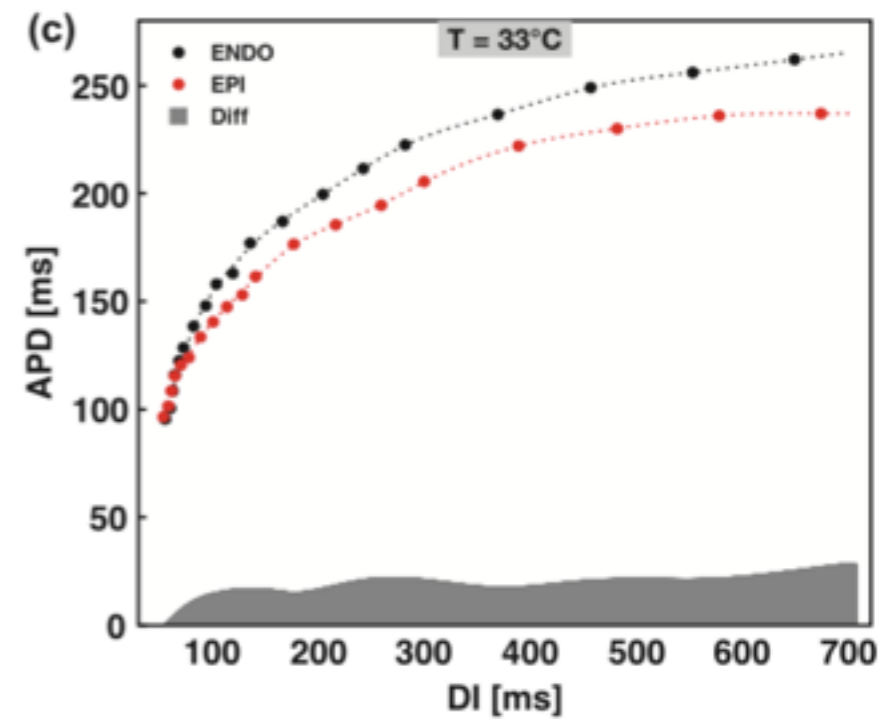
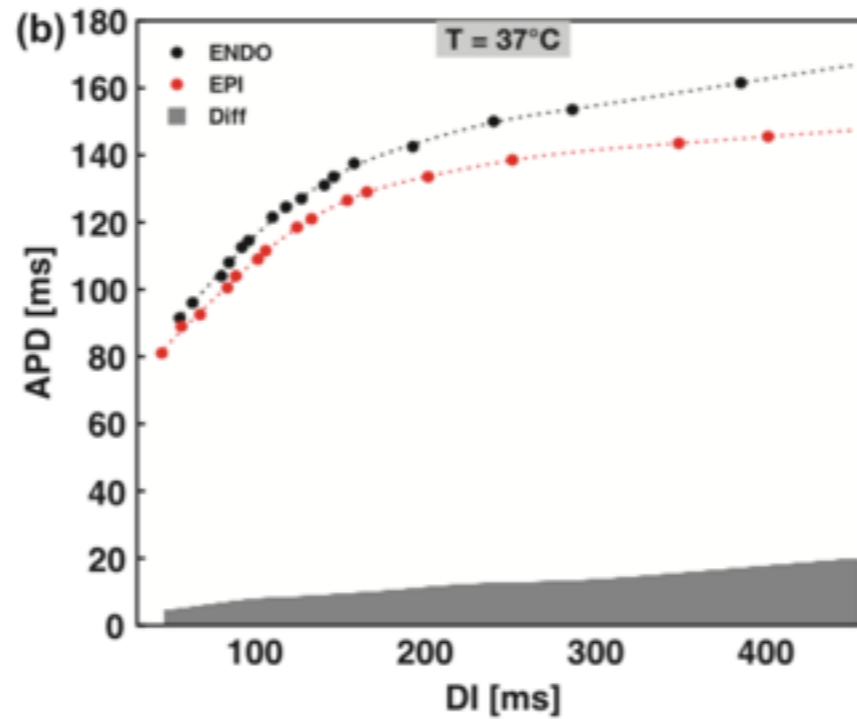
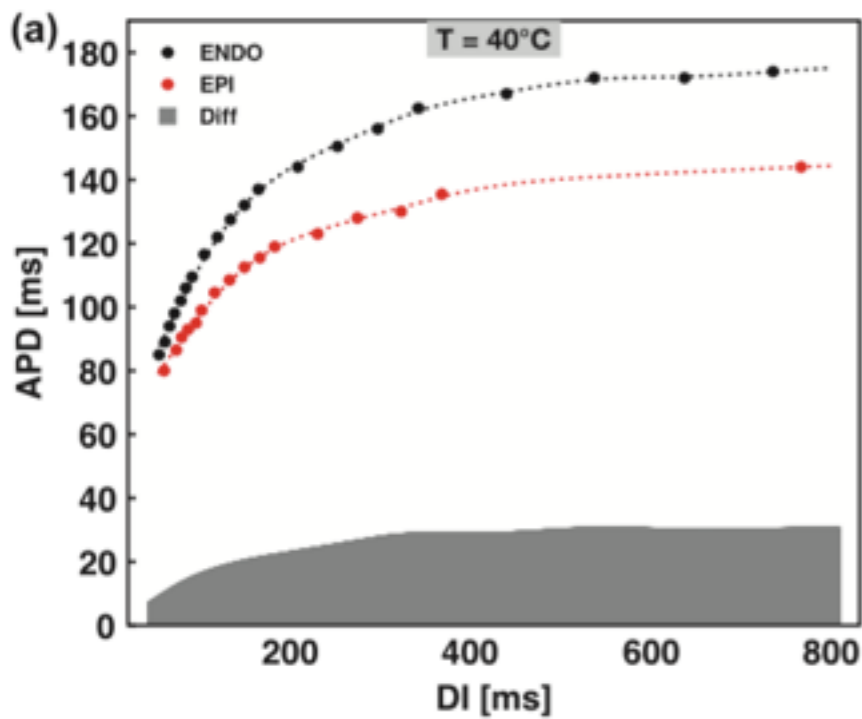


# Model Tuning

## Restitution Curve Fitting



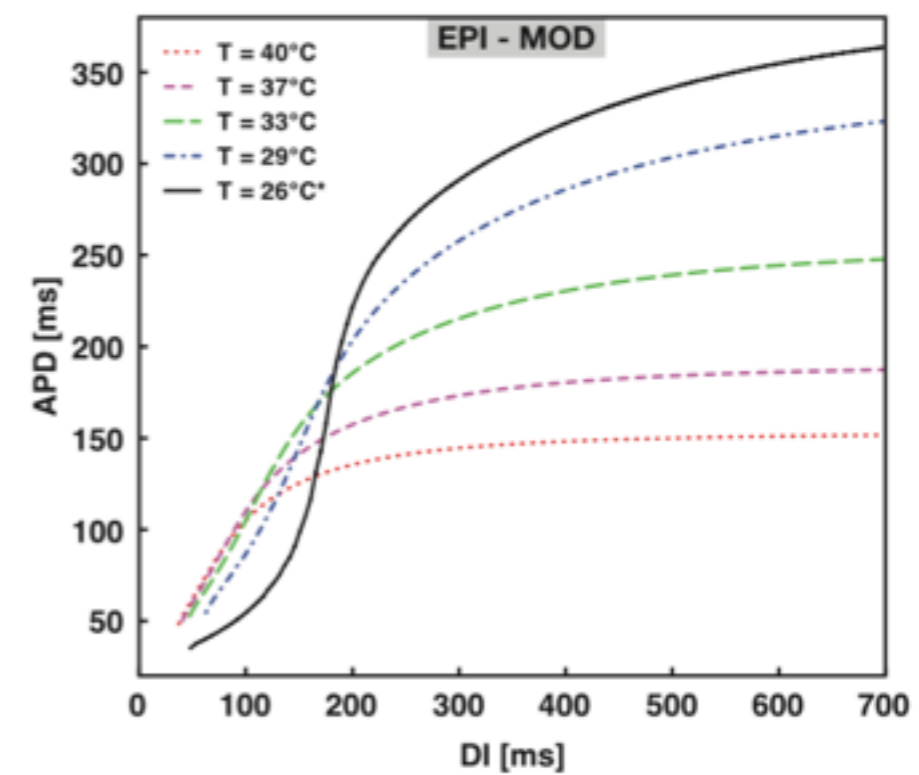
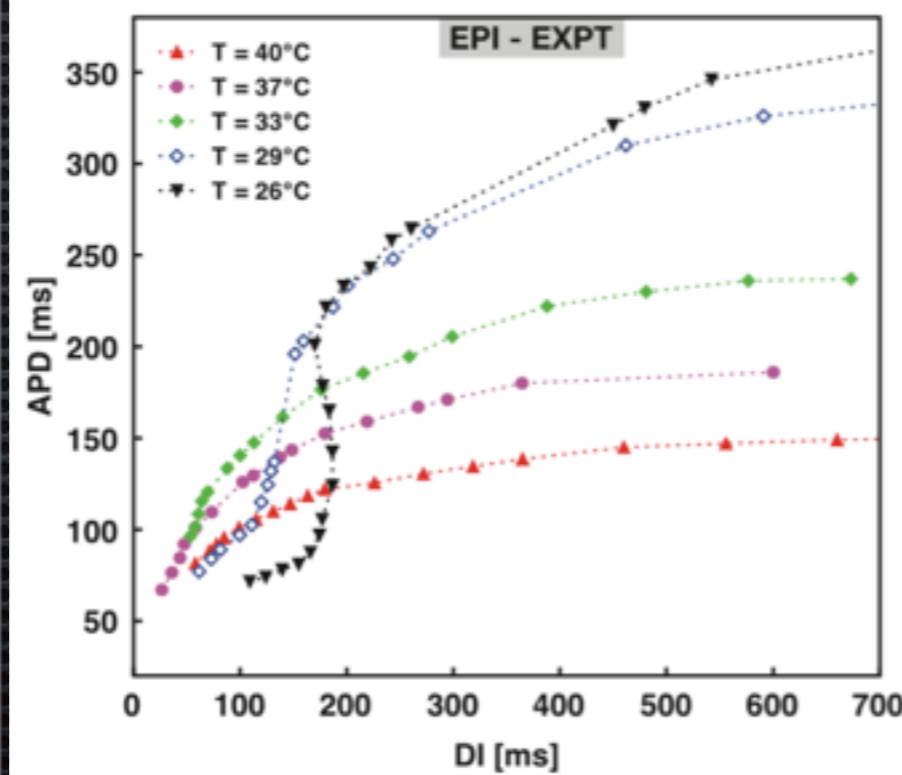
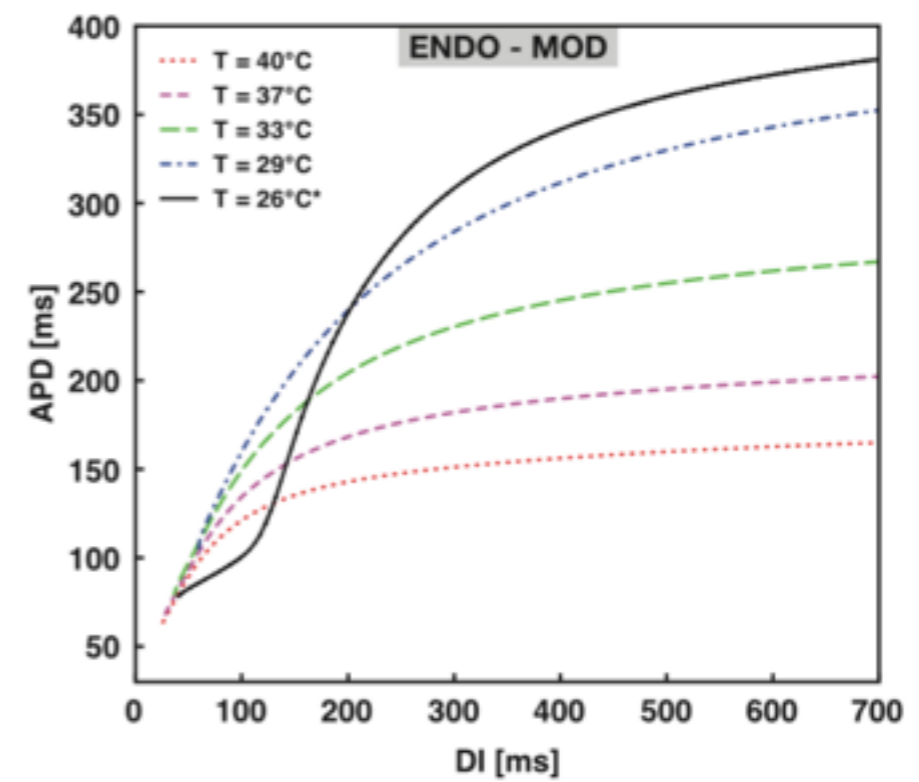
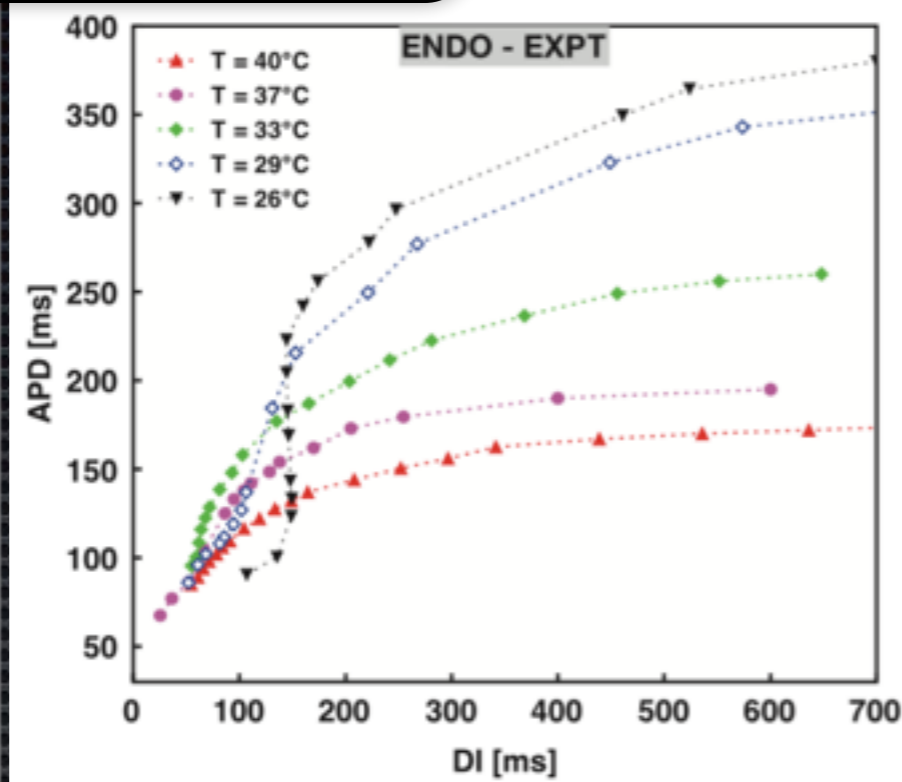
Intramural dispersion



Different  
time  
constants

# Model Tuning

## Restitution Curve Fitting

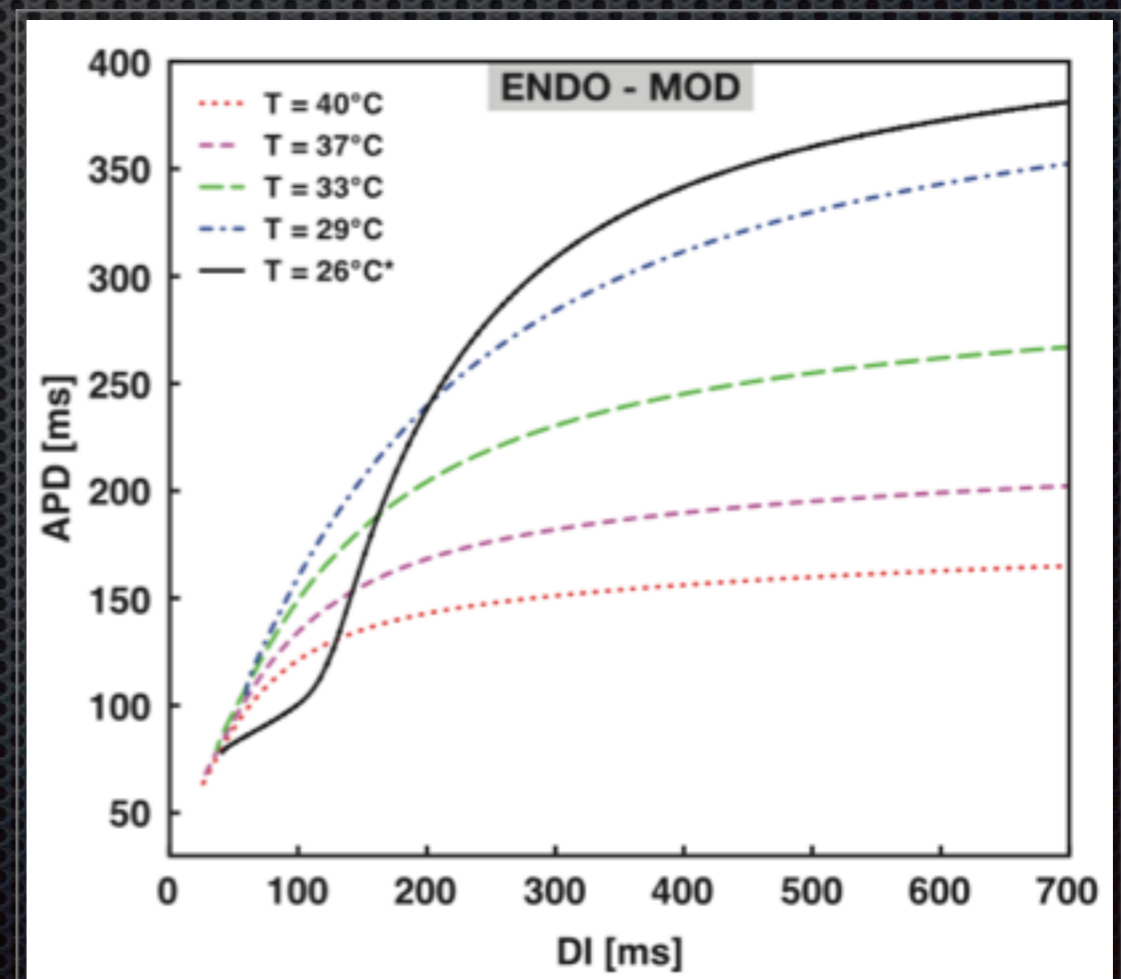


# Model Tuning

## Optimal Set of Parameters

EPI <sub>29-40</sub>	ENDO <sub>29-40</sub>	EPI <sub>26</sub>	ENDO <sub>26</sub>
$u_o = 0$	0	0	0
$u_w = 1.55$	1.56	1.55	1.56
$\theta_v = 0.3$	0.3	0.3	0.3
$\theta_w = 0.13$	0.13	0.13	0.13
$\theta_v^- = 0.006$	0.2	0.006	0.2
$\theta_o = 0.006$	0.006	0.006	0.006
$\tau_v^+ = 1.4506$	1.4506	1.4506	1.4506
$\tau_{v1}^- = 20$	55	10	15
$\tau_{v2}^- = 1150$	40	1150	40
$\tau_{w1}^- = 120$	40	75	40
$\tau_{w2}^- = 300$	115	90	165
$\tau_{w1}^+ = 120$	175	90	175
$\tau_{w2}^+ = 140$	230	140	150
$k_w^- = 65$	20	65	8000
$u_w^- = 0.03$	0.00615	0.02	0.005
$k_w^+ = 5.7$	8	6.5	8
$u_w^+ = 0.15$	0.0005	0.8	0.0005
$\tau_{fi} = 0.11$	0.10	0.11	0.10
$\tau_{o1} = 400$	470	400	470
$\tau_{o2} = 6$	6	6	6
$\tau_{so1} = 30.0181$	40	30.0181	40
$\tau_{so2} = 0.9957$	1.2	0.9957	1.2
$k_{so} = 2.0458$	2	2.0458	2
$u_{so} = 0.65$	0.65	0.65	0.65
$\tau_{s1} = 2.7342$	2.7342	2.7342	2.7342
$\tau_{s2} = 16$	2	16	2
$k_s = 2.0994$	2.0994	2.0994	2.0994
$u_s = 0.9087$	0.9087	0.9087	0.9087
$\tau_{si} = 1.8875$	2.9013	1.8875	2.9013
$\tau_{w\infty} = 0.07$	0.0273	0.07	0.0273
$w_{\infty}^* = 0.94$	0.78	0.94	0.78
$Q_{10,v} = 1.5$	1.5	0.9	1.5
$Q_{10,w} = 2.45$	2.45	3	2.5
$Q_{10,s} = 1.5$	1.5	1.35	1.5
$A_{fi} = 1$	1	2	1.5
$B_{fi} = 0.065$	0.065	0.065	0.065
$A_{so} = 1$	1	1.4	1
$B_{so} = 0.008$	0.008	0.008	0.008
$A_{si} = 1$	1	1.4	1
$B_{si} = 0.008$	0.008	0.008	0.008

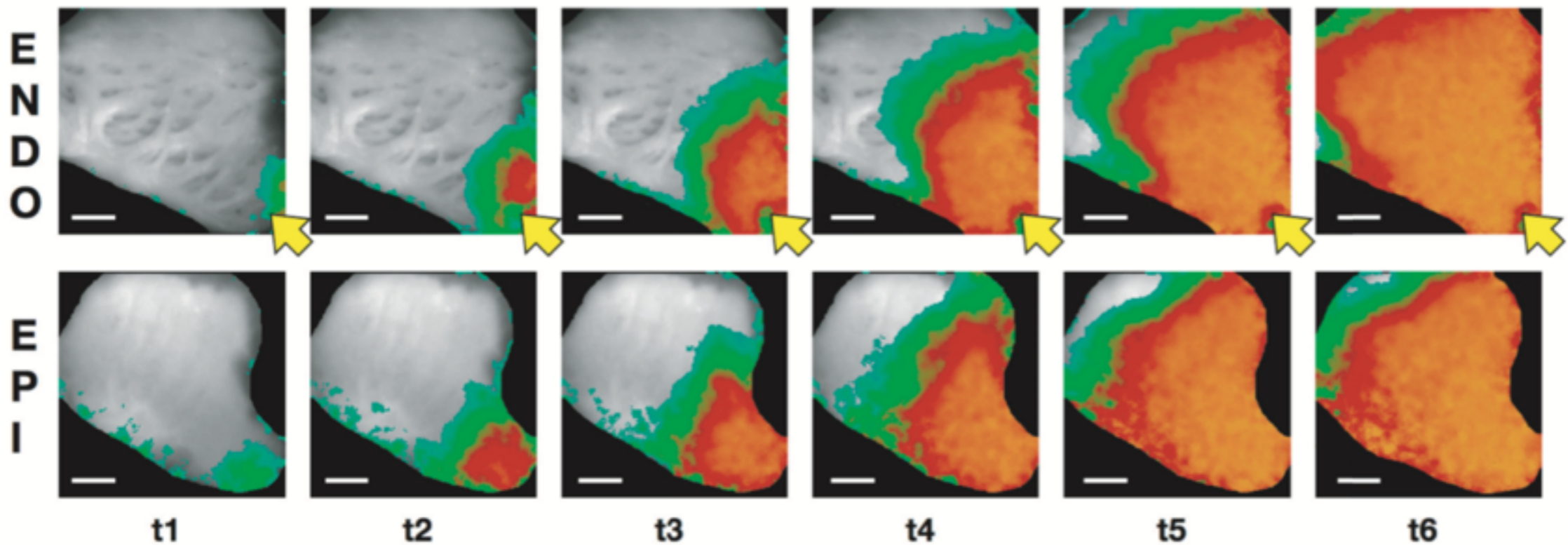
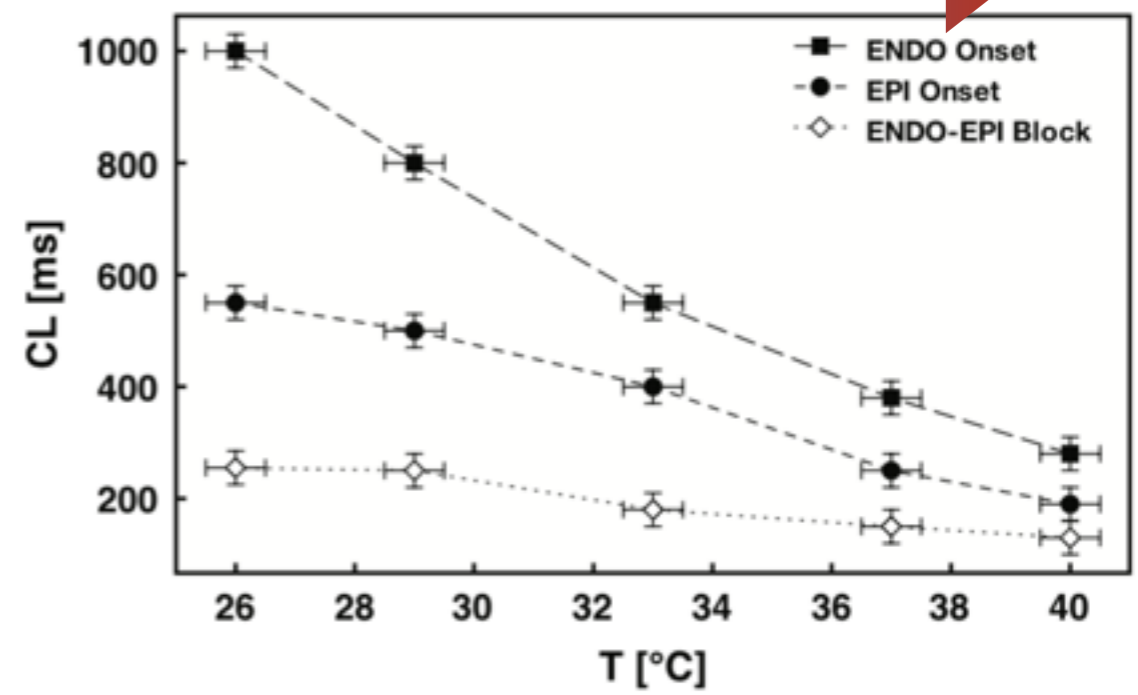
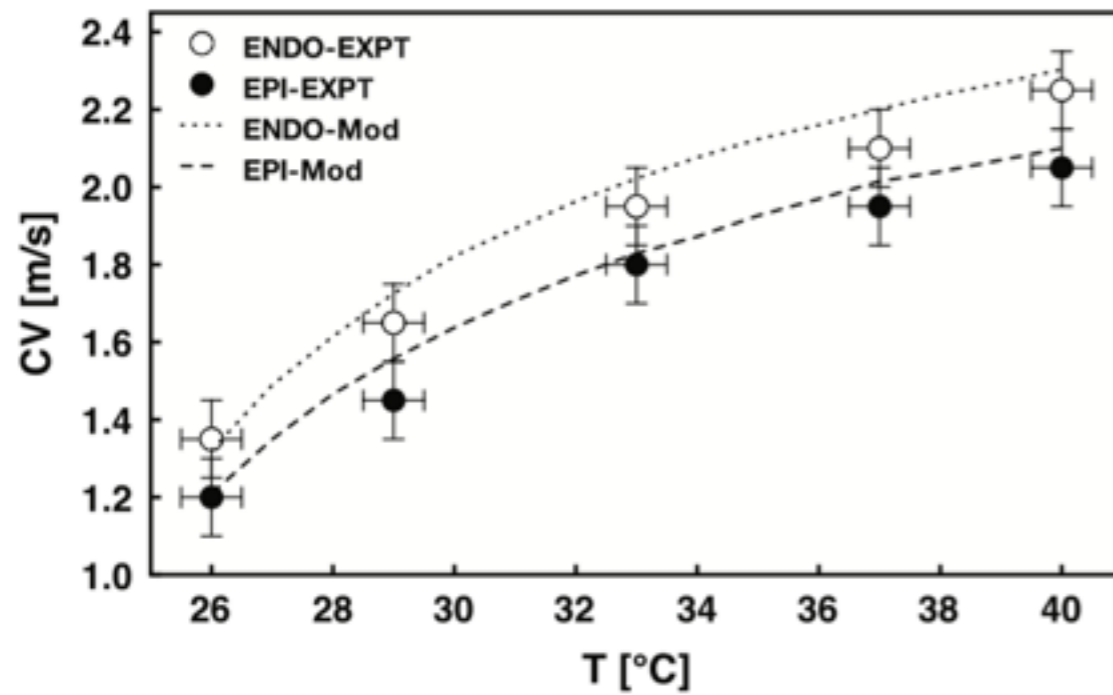
Curve	$p$	$R$ square
ENDO <sub>29</sub>	$2.3730462 \times 10^{-5}$	0,9991
ENDO <sub>33</sub>	$4.7727621 \times 10^{-4}$	0,9987
EPI <sub>29</sub>	$1.1400597 \times 10^{-4}$	0,9956
EPI <sub>33</sub>	$4.2275630 \times 10^{-4}$	0,9989
EPI <sub>40</sub>	$1.6385054 \times 10^{-4}$	0,9988





# Model Tuning

## Spatio-Temporal Features



# Bifurcation Analysis

Idea: circuit length reduction during single AP propagation

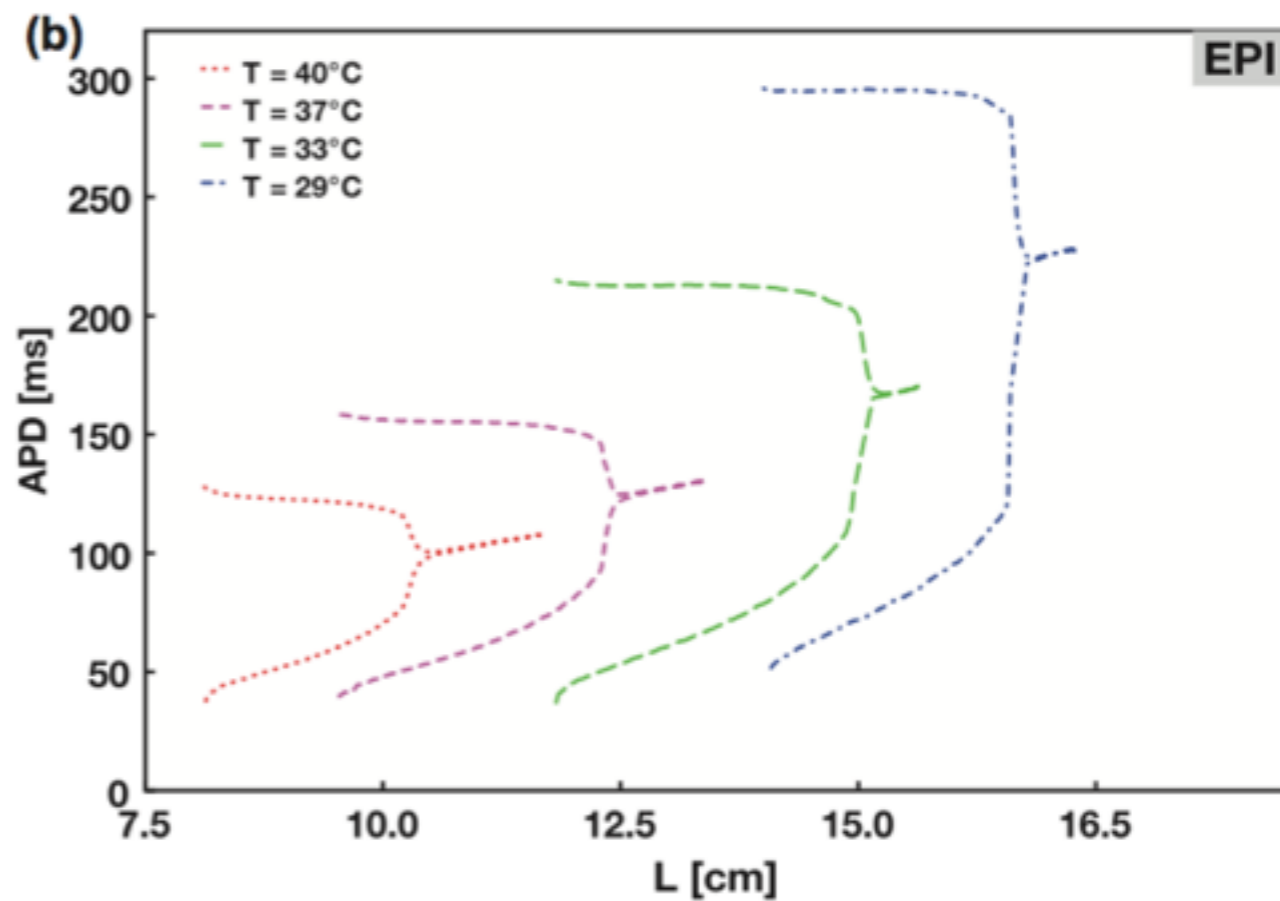
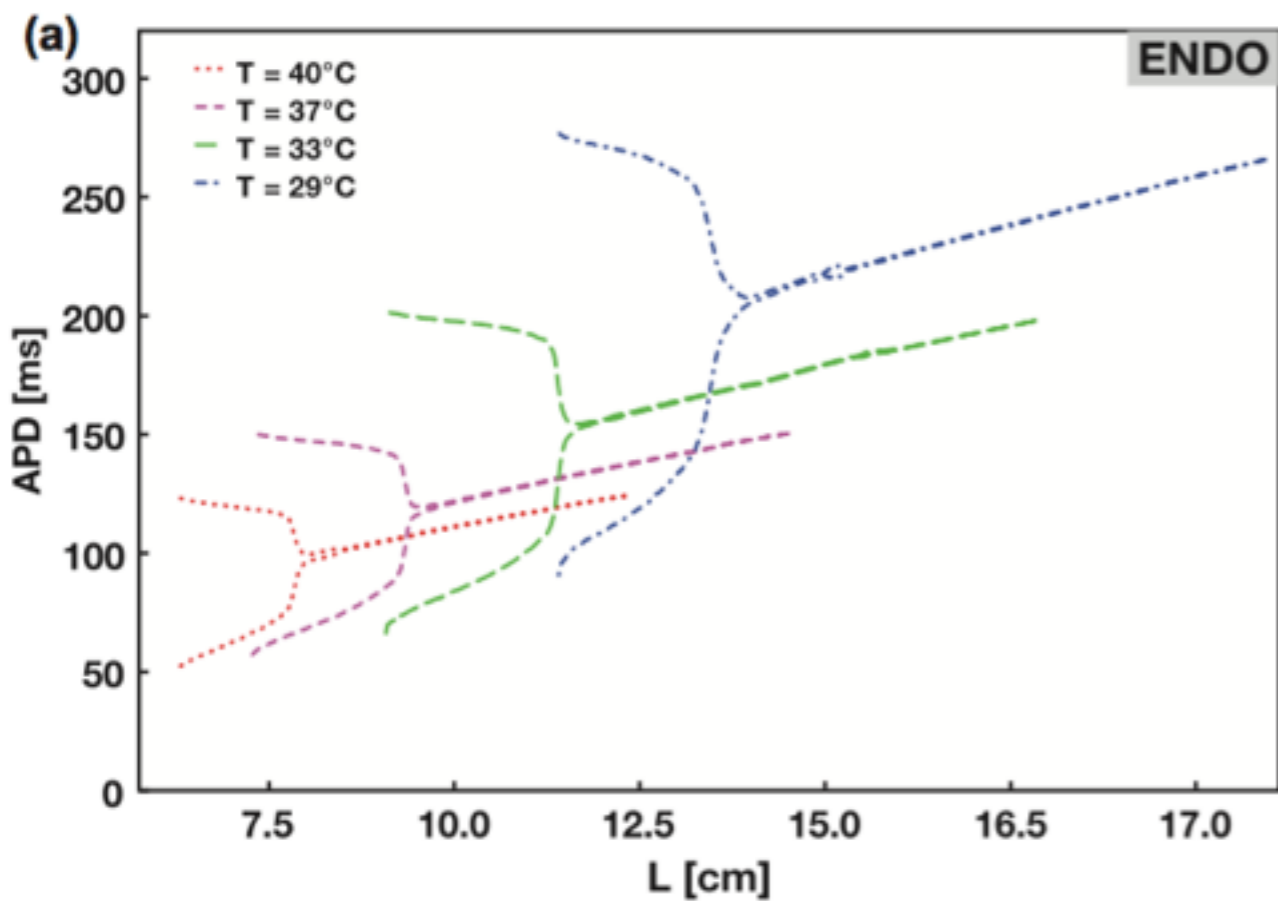


**Induction of  
Alternans**

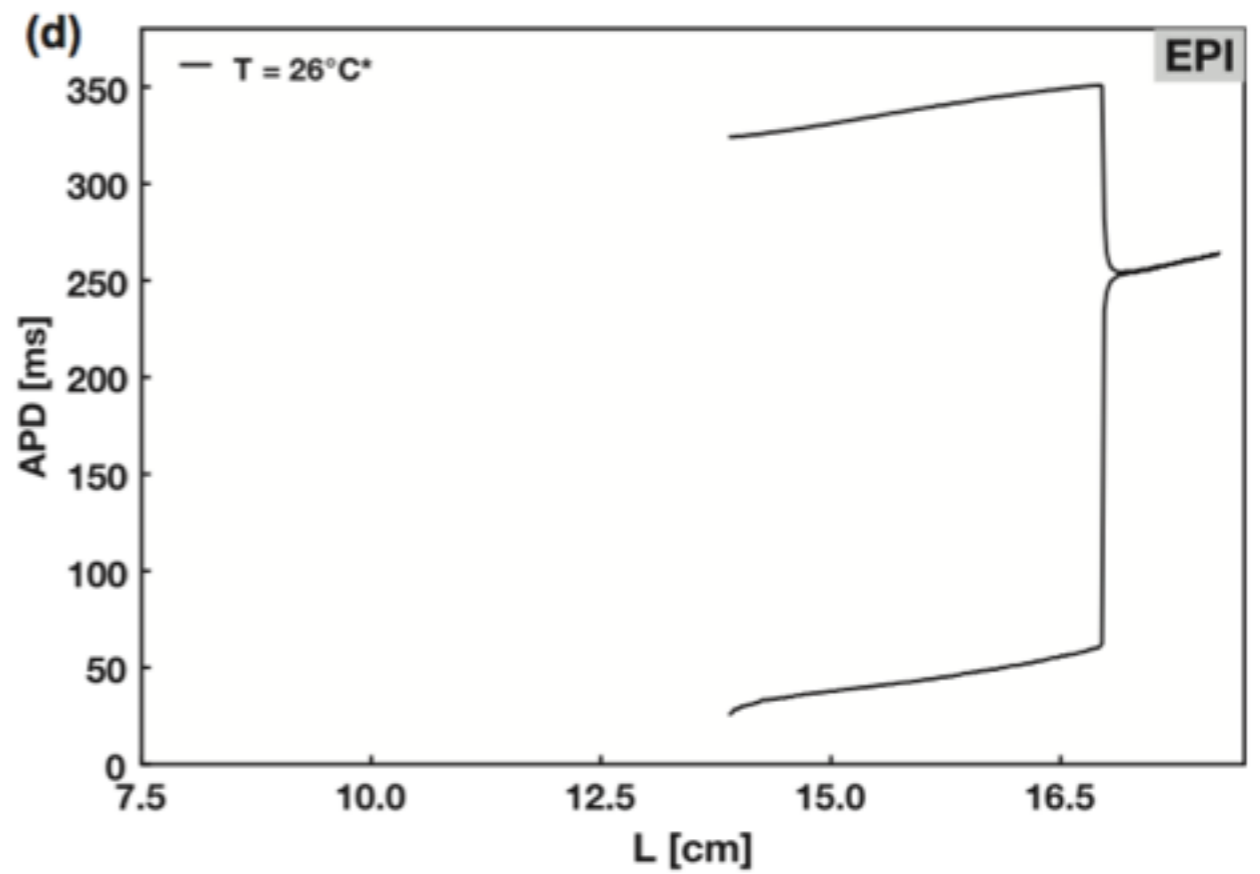
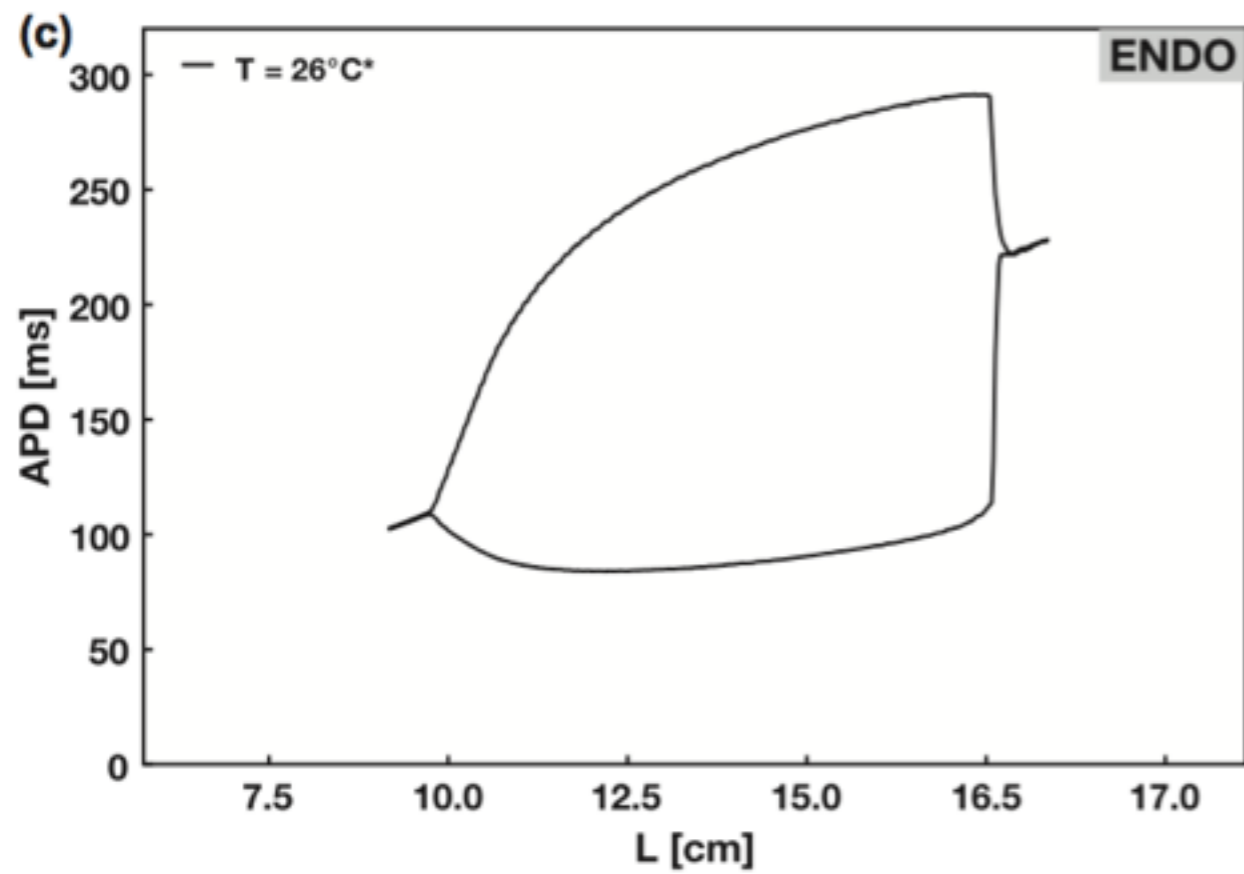
Sun, J., Amellal, F., Glass, L., & Billette, J. (1995). *Journal of theoretical biology*, 173(1), 79-91.

Winfree, Arthur T. *The geometry of biological time*. Vol. 12. Springer Science & Business Media, 2001.

# Bifurcation Analysis

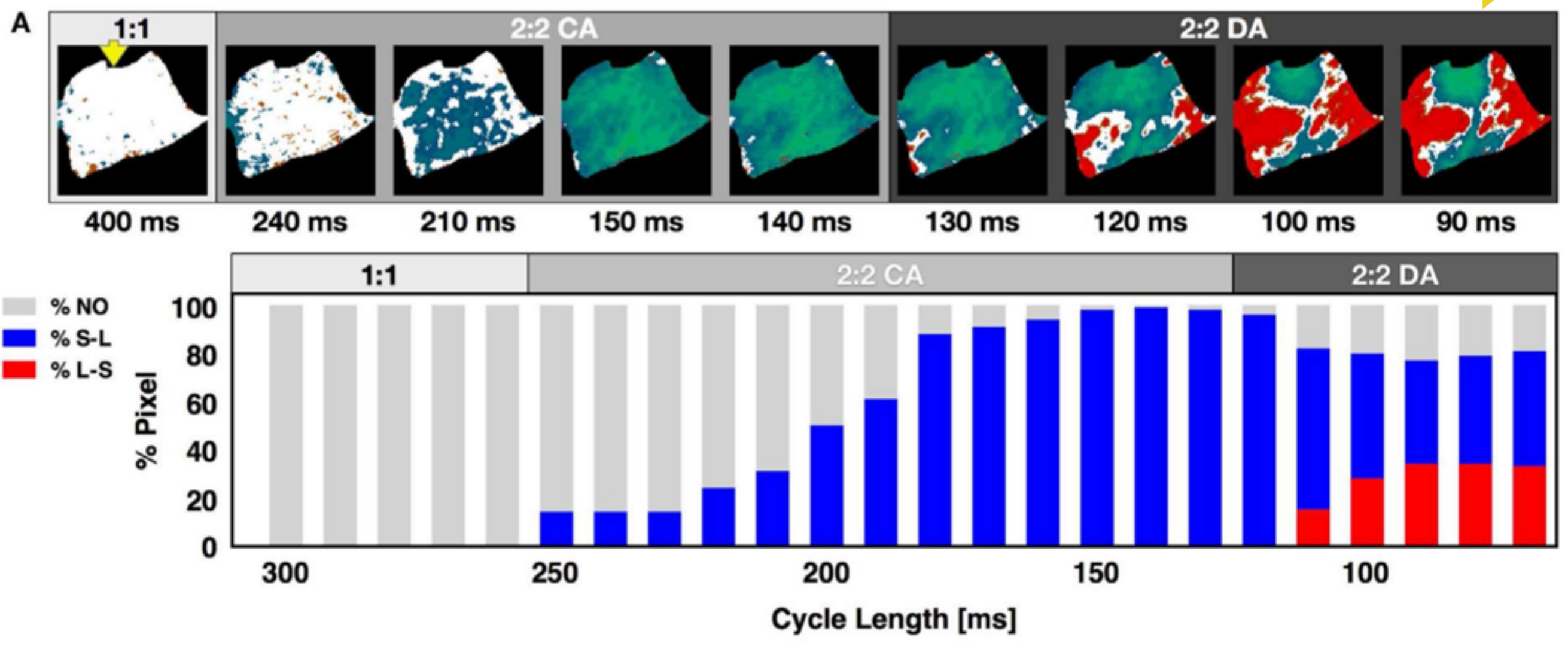


# Bifurcation Analysis



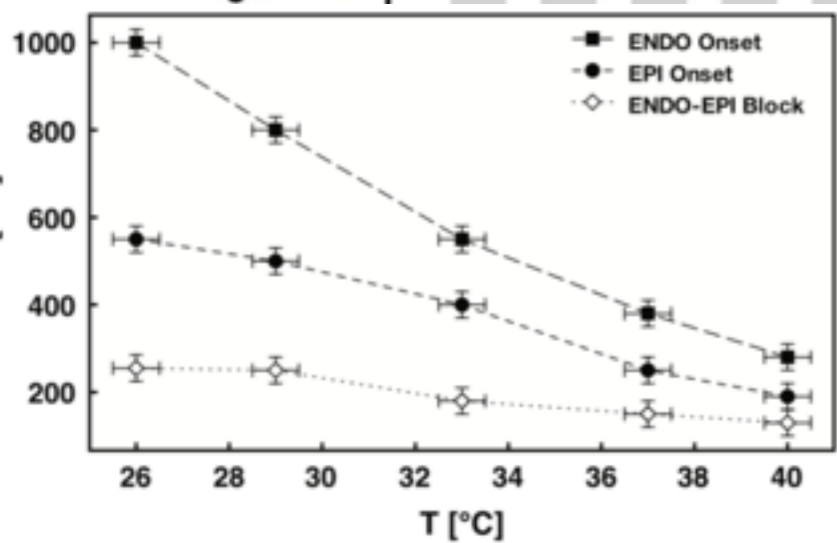
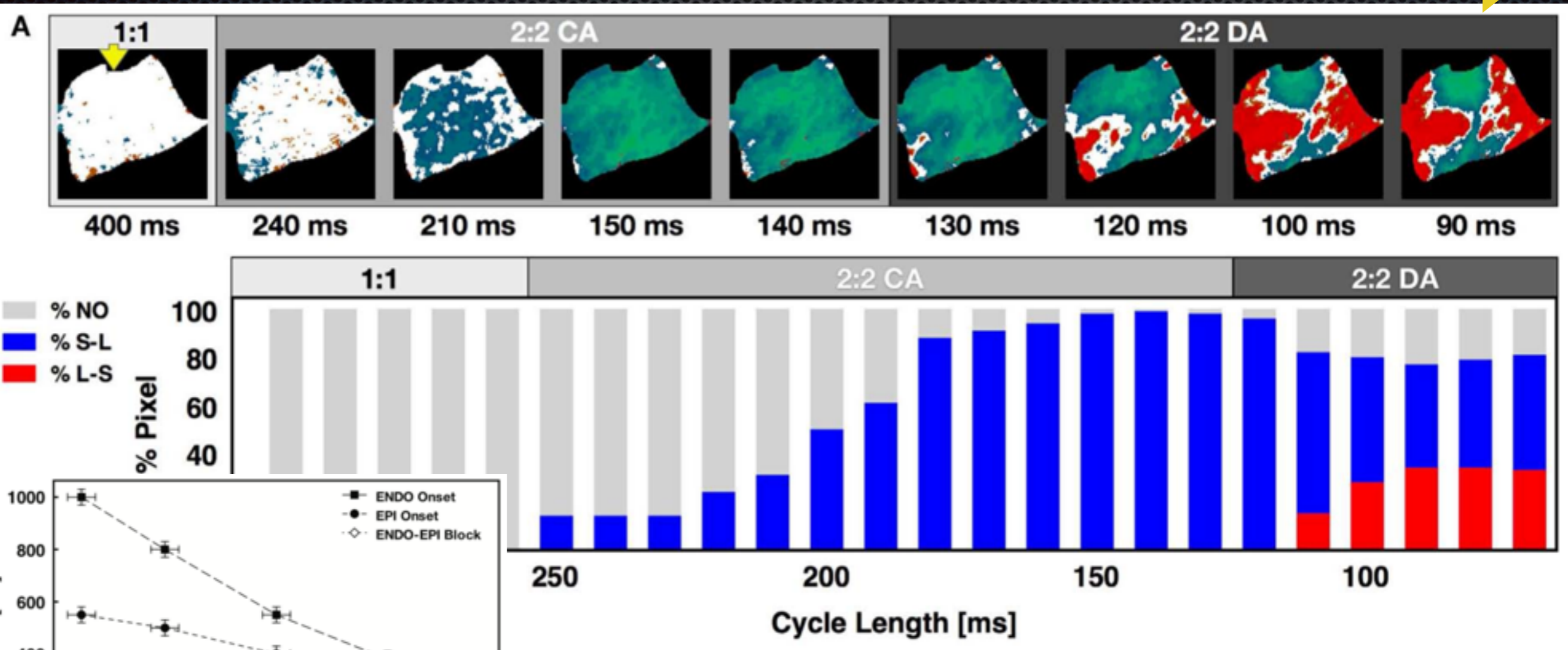
# Spatio-Temporal Bifurcation

## Alternans Patterns Onset and Development



# Spatio-Temporal Bifurcation

## Alternans Patterns Onset and Development

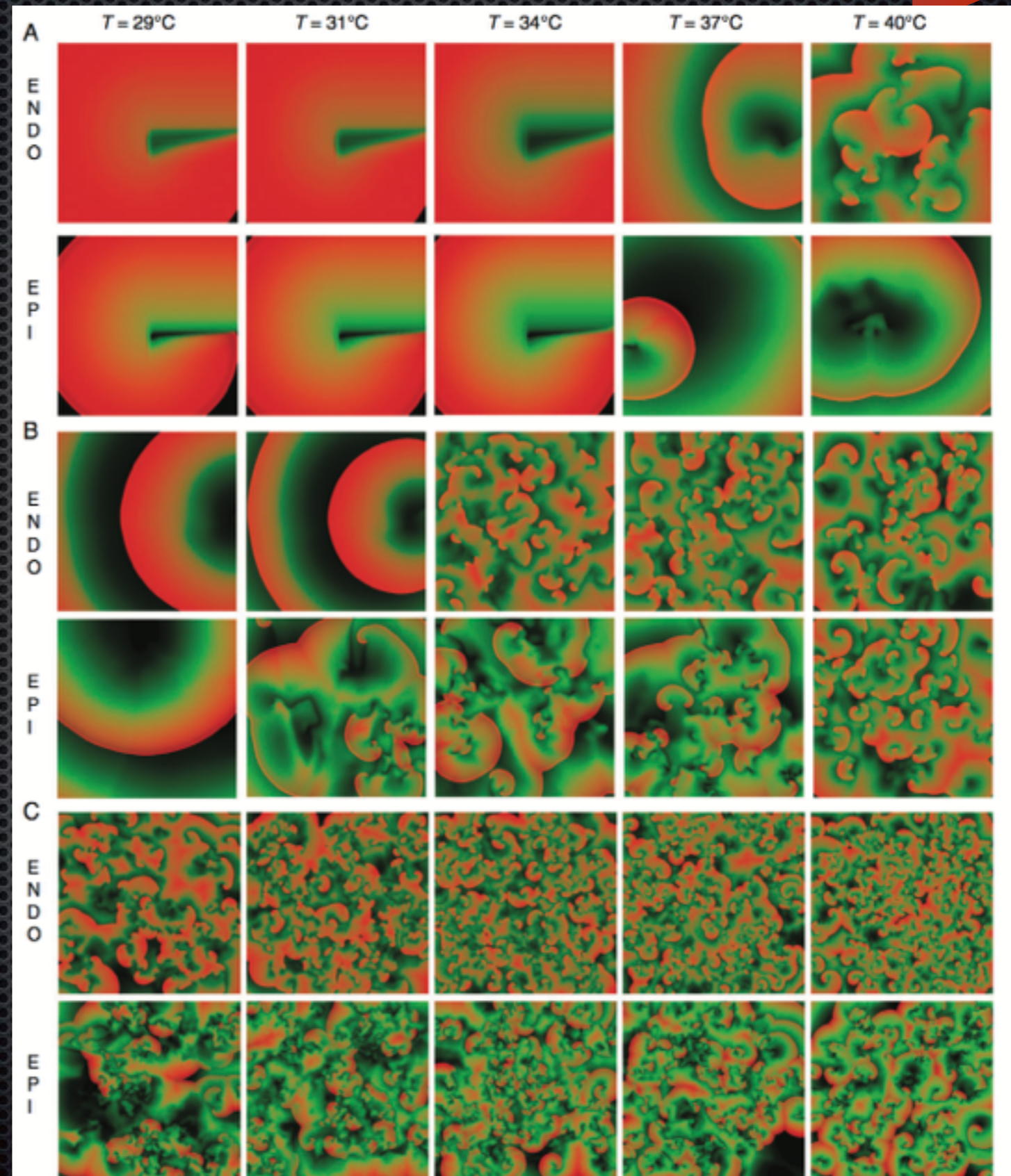


# Size Effect Analysis

Effect of the domain size on the sustenance of arrhythmias (spirals)

Tissue model	40°C	37°C	34°C	31°C	29°C
EPI 2.5 × 2.5 cm <sup>2</sup>	NS	NS	NS	NS	NS
EPI 3.2 × 3.2 cm <sup>2</sup>	NS	NS	NS	NS	NS
EPI 6.4 × 6.4 cm <sup>2</sup>	S	S	S	NS	NS
EPI 12.8 × 12.8 cm <sup>2</sup>	S	S	S	S	S
ENDO EPI 2.5 × 2.5 cm <sup>2</sup>	S	NS	NS	NS	NS
ENDO 3.2 × 3.2 cm <sup>2</sup>	S	S	NS	NS	NS
ENDO 6.4 × 6.4 cm <sup>2</sup>	S	S	S	NS	NS
ENDO 12.8 × 12.8 cm <sup>2</sup>	S	S	S	S	S

GPU - WebGL



Eurpace (2014) 16, 424–434  
doi:10.1093/eurpace/euu031

FOCUSED ISSUE: ORIGINAL RESEARCH

## Mechanistic insights into hypothermic ventricular fibrillation: the role of temperature and tissue size

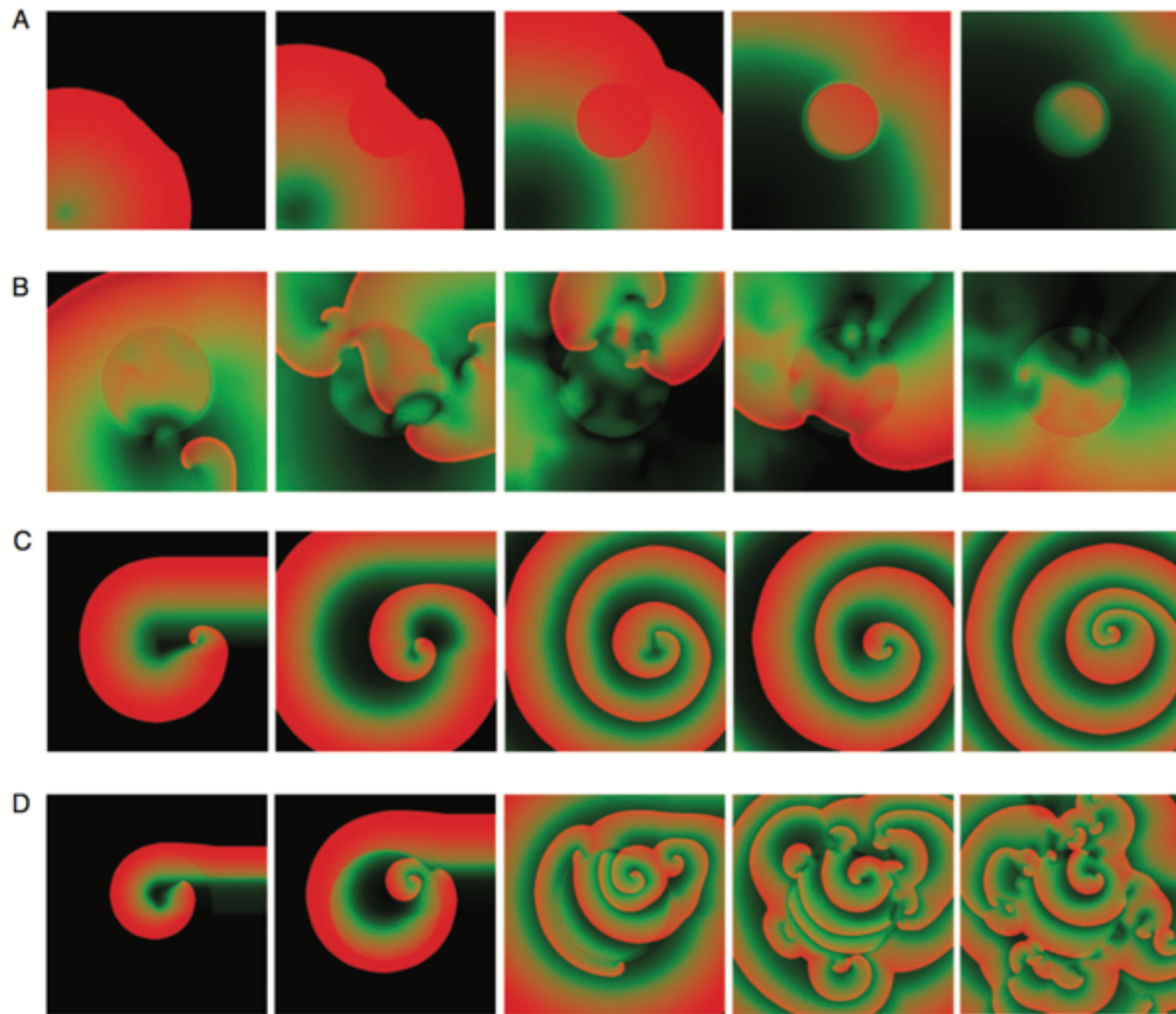
Simonetta Filippi<sup>1,2\*</sup>, Alessio Gizzi<sup>1,2</sup>, Christian Cherubini<sup>1,2</sup>, Stefan Luther<sup>3</sup> and Flavio H. Fenton<sup>4\*</sup>

<sup>1</sup>Nonlinear Physics and Mathematical Modeling Laboratory, University Campus Bio-Medico of Rome, Via A. del Portillo 21, I-00128 Rome, Italy; <sup>2</sup>International Center for Relativistic Astrophysics—ICRA, University Campus Bio-Medico of Rome, Via A. del Portillo 21, I-00128 Rome, Italy; <sup>3</sup>Max Planck Institute for Dynamics and Self-Organization, Am Fassberg 17, D-37077 Göttingen, Germany; and <sup>4</sup>School of Physics, Georgia Institute of Technology, 807 State Street, Atlanta, GA 30332, USA

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# Regional Cooling

time



Tissue 37°C - Disc 29°C  
Disc radius: 0.4 cm  
Domain: 2.5 cm x 2.5 cm

Tissue 37°C - Disc 29°C  
Disc radius: 0.8 cm  
Domain: 3.2 cm x 3.2 cm

Tissue 40°C - No Cooling  
Domain: 6.4 cm x 6.4 cm

Tissue 40°C - Disc 29°C  
Disc radius: 1.6 cm  
Domain: 6.4 cm x 6.4 cm



## Conclusions

- **Temporal dynamics:** temperature affects significantly action potential shape and restitution curves.
- **Spatio-temporal dynamics:** alternans onset (affected by conduction velocity and pacing frequency) depends on temperature.
- **Tissue and temperature effects:** sustenance of arrhythmias is clearly affected by the mixed effects of tissue size and temperature.
- **Thermal treatment:** localised hypothermic treatment affects fibrillation sustenance...

9th meeting of

European  
Study  
Group on  
Cardiovascular  
Oscillations



# Thank You for Your Attention

Alessandro Loppini

Christian Cherubini, Simonetta Filippi, Alessio Gizzi

University Campus Bio-Medico of Rome

Nonlinear Physics and Mathematical Modeling Laboratory

&

Flavio H. Fenton

Georgia Institute of Technology



Georgia  
Tech

